# CS738: Advanced Compiler Optimizations Pointer Analysis

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#### Static analysis of pointers & references



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#### Static analysis of pointers & references



Statement S8 is not redundant.

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#### Reaching definitions analysis

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#### Reaching definitions analysis





#### Flow Sensitive Analysis

 Order of execution: Determined by the semantics of language

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  - Kill component in the flow function

Flow Insensitive Analysis

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 Order of execution: Statements are assumed to execute in any order

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"Summary" for the procedure

#### Flow Insensitive Analysis

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  - Summary" for the procedure
  - Safe approximation of flow-sensitive point-specific information for any point, for any given execution order
- A statement can not "override" information computed by another statement
  - NO Kill component in the flow function
  - If statement s kills some data flow information, there is an alternate path that excludes s

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Type checking, Type inferencing

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#### Type checking, Type inferencing

Compute/Verify type of a variable/expression

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Address taken analysis

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  - Which variables have their addresses taken?

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A very simple form of pointer analysis

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- Side effects analysis

#### Type checking, Type inferencing

- Compute/Verify type of a variable/expression
- Address taken analysis
  - Which variables have their addresses taken?
  - A very simple form of pointer analysis
- Side effects analysis
  - Does a procedure modify address / global variable / reference parameter / ...?



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Allows arbitrary compositions of flow functions in any order  $\Rightarrow$  Flow insensitivity

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In practice, dependent constraints are collected in a global repository in one pass and solved independently

Points-to Analysis	Alias Analysis
x = &a	x = a
x points-to a	x and a are aliases

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Reflexive?		

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Reflexive?	No	Yes

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<b>Reflexive?</b>	No	Yes
Symmetric?		

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<b>Reflexive?</b>	No	Yes
Symmetric?	No	Yes

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Reflexive?	No	Yes
Symmetric?	No	Yes
Transitive?		

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Alias Analysis vs. Points-to Analysis

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Reflexive?	No	Yes
Symmetric?	No	Yes
Transitive?	No	Must alias: Yes, May alias: No

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Subset based analysis



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• Equality based analysis:  $P_{lhs} \equiv P_{rhs}$ 

 Only one Points-to successor at any time, merge (potential) multiple successors



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$$a = \&b$$



$$a = \&b$$

$$a \longrightarrow b$$

$$b = \&c$$

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Equality based



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# **Pointer Indirection Constraints**

Stmt	Subset based	Equality based
a = *b	$P_a \supseteq P_c, \forall c \in P_b$	$MERGE(P_a, P_c), \forall c \in P_b$
*a = b	$P_{c} \supseteq P_{b}, \forall c \in P_{a}$	$MERGE(P_b, P_c), \forall c \in P_a$

## Must Points-to Analysis



• x definitely points-to a at various points in the program •  $x \xrightarrow{D} a$ 

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## May Points-to Analysis



- At OUT of 2, x definitely points-to b
- At OUT of 3, x definitely points-to a
- At IN of 4, x possibly points-to a (or b)

$$\blacktriangleright x \xrightarrow{P} a, x \xrightarrow{P} b$$

## May Points-to Analysis



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 $\triangleright x \xrightarrow{P} \{a, b\}$ 

#### **Must Alias Analysis**



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• x and a always refer to same memory location •  $x \stackrel{\text{D}}{=} a$ 

### **Must Alias Analysis**



- *x* and *a* always refer to same memory location
   *x* <sup>b</sup> = *a*
- x, y and a refer to same location at OUT of 4. •  $x \stackrel{\text{\tiny D}}{=} y \stackrel{\text{\tiny D}}{=} a$



- At OUT of 2, x and b are must aliases
- At OUT of 3, x and a are must aliases
- At IN of 4, x can *possibly* be aliased with either a (or b)
   x <sup>p</sup>/<sub>=</sub> a, x <sup>p</sup>/<sub>=</sub> b



- At OUT of 2, x and b are must aliases
- At OUT of 3, x and a are must aliases
- At IN of 4, x can *possibly* be aliased with either a (or b)
   (x, a), (x, b)

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If we say: (x, a, b), Is it Precise?



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   (x, a), (x, b)

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If we say: (x, a, b), Is it Precise? Safe?
Makes sense only for Flow Sensitive analysis



Makes sense only for Flow Sensitive analysis

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► Why?

Makes sense only for Flow Sensitive analysis

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- ► Why?
- ► Must analysis ⇒ Flow sensitive analysis

- Makes sense only for Flow Sensitive analysis
- Why?
- ► Must analysis ⇒ Flow sensitive analysis
- ► Flow insensitive analysis ⇒ May analysis

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- Makes sense only for Flow Sensitive analysis
- Why?
- ► Must analysis ⇒ Flow sensitive analysis
- ► Flow insensitive analysis ⇒ May analysis

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► Why?

Never if flow insensitive analysis

- Never if flow insensitive analysis
- For flow sensitive



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x, y may or may not get modified in 5: Weak update



x, y may or may not get modified in 5: Weak update

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c definitely gets modified in 5: Strong update



- x, y may or may not get modified in 5: Weak update
- c definitely gets modified in 5: Strong update
- Must information is killed by Strong and Weak updates



For flow sensitive



- x, y may or may not get modified in 5: Weak update
- c definitely gets modified in 5: Strong update
- Must information is killed by Strong and Weak updates
- May information is killed only by Strong updates

Basic statements for pointer manipulation

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Basic statements for pointer manipulation

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Basic statements for pointer manipulation

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Other statements can be rewritten in terms of above

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•  $x = NULL \Rightarrow$  treat NULL as a special variable

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Other statements can be rewritten in terms of above

$$x = *y \Rightarrow t = *y, *x = t$$

•  $x = NULL \Rightarrow$  treat NULL as a special variable

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$$OUT = IN - kill \cup gen$$

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$$\mathbf{k} \mathbf{x} = \mathbf{x} \mathbf{y} \Rightarrow \mathbf{t} = \mathbf{x} \mathbf{y}, \ \mathbf{x} = \mathbf{t} \mathbf{y}$$

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with a twist!

Flow Function: x = y

$$\begin{array}{lll} \mathsf{May}_{gen} & = & \{x \rightarrow p \mid y \rightarrow p \in \mathsf{May}_{\mathit{IN}}\} \\ \mathsf{May}_{\mathit{kill}} & = & \bigcup_{p \in \mathit{Vars}} \{x \rightarrow p\} \end{array}$$

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Flow Function: x = y

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Flow Function: x = &y

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Flow Function: \*x = y

$$\begin{aligned} \mathsf{May}_{gen} &= \{ p \to p' \mid x \to p \in \mathsf{May}_{IN}, y \to p' \in \mathsf{May}_{IN} \} \\ \mathsf{May}_{kill} &= \bigcup_{p' \in \mathsf{Vars}} \{ p \to p' \mid x \to p \in \mathsf{Must}_{IN} \} & \underbrace{\mathsf{Strong update}_{II}} \\ \mathsf{Must}_{gen} &= \{ p \to p' \mid x \to p \in \mathsf{Must}_{IN}, y \to p' \in \mathsf{Must}_{IN} \} \\ \mathsf{Must}_{kill} &= \bigcup_{p' \in \mathsf{Vars}} \{ p \to p' \mid x \to p \in \mathsf{May}_{IN} \} & \underbrace{\mathsf{Weak update}_{II}} \end{aligned}$$

$$\mathsf{Must}_{kill} = \bigcup_{p' \in Vars} \{p \to p' \mid x \to p \in \mathsf{May}_{IN}\}$$

May Points-To analysis

#### May Points-To analysis

A points-to pair should be removed only if it must be removed along all paths

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# Summarizing Flow Functions

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- ► Must Points-To ⊆ May Points-To

# Safe Approximations for May and Must Points-to

### A pointer variable

	Мау	Must
Points-to	points to every possible	points to nothing
	location	
Alias	aliased to every other	only to itself
	pointer variable	

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Non-Distributivity of Points-to Analysis



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