Agenda CS738: Advanced Compiler Optimizations Static Single Assignment (SSA) SSA Form Amey Karkare karkare@cse.iitk.ac.in Constructing SSA form Properties and Applications http://www.cse.iitk.ac.in/~karkare/cs738 Department of CSE, IIT Kanpur SSA Form What is SSA Form? Developed by Ron Cytron, Jeanne Ferrante, Barry K. An Intermediate Representation Rosen, Mark N. Wegman, and F. Kenneth Zadeck, Sparse representation ▶ in 1980s while at IBM. Definitions sites are directly associated with use sites Static Single Assignment – A variable is assigned only Advantage once in program text Directly access points where relevant data flow information May be assigned multiple times if program is executed is available

SSA IR

Example







Computing Dominators

Equation

$$DOM(n) = \{n\} \cup \left(\bigcap_{m \in PRED(n)} DOM(m)\right), \\ \forall n \in N$$

Initial Conditions:

 $DOM(n_{Entry}) = \{n_{Entry}\}$ $DOM(n) = N, \forall n \in N - \{n_{Entry}\}$

where N is the set of all nodes, n_{Entry} is the node corresponding to the *Entry* block.

Note that efficient methods exist for computing dominators

Dominator Tree Example



Immediate Dominators and Dominator Tree

- x is immediate dominator of y if x is the closest strict dominator of y
 - unique, if it exists
 - denoted idom[y]
- Dominator Tree
 - A tree showing all immediate dominator relationships

Dominance Frontier: DF

- Dominance Frontier of x is set of all nodes y s.t.
 - x dominates a predecessor of y AND
 - x does not strictly dominate y
- Denoted DF(x)
- ▶ Why do you think DF(*x*) is important for any *x*?
 - ► Think about the information originated in *x*.

Computing DF

- PARENT(x) denotes parent of node x in the dominator tree.
- CHILDERN(x) denotes children of node x in the dominator tree.
- PRED and SUCC from CFG.

$$\mathsf{DF}(x) = \mathsf{DF}_{\mathsf{local}}(x) \cup \left(\bigcup_{z \in \mathsf{CHILDERN}(x)} \mathsf{DF}_{\mathsf{up}}(z)\right)$$

 $\begin{array}{lll} \mathsf{DF}_{\mathsf{local}}(x) & = & \{y \in \mathsf{SUCC}(x) \mid \mathsf{idom}[y] \neq x \} \\ & \mathsf{DF}_{\mathsf{up}}(z) & = & \{y \in \mathsf{DF}(z) \mid \mathsf{idom}[y] \neq \mathsf{PARENT}(z) \} \end{array}$

Iterated Dominance Frontier

- Transitive closure of Dominance frontiers on a set of nodes
- ► Let *S* be a set of nodes

$$DF(S) = \bigcup_{x \in S} DF(x)$$
$$DF^{1}(S) = DF(S)$$
$$DF^{i+1}(S) = DF(S \cup DF^{i}(S))$$

• $DF^+(S)$ is the fixed point of DF^i computation.

Inserting ϕ -functions

```
    Compute DF<sup>+</sup> set for each flow graph node
    Place trivial φ-functions for each variable in the node
    trivial φ-function at n-ary join: x = φ(x, x, ..., x)
```

- Rename variables
- ► Why DF⁺? Why not only DF?

Minimal SSA Form Construction

```
foreach variable v \in S = Entry \cup \{B_n \mid v \text{ defined in } B_n\}
Compute \mathsf{DF}^+(S)
foreach n in \mathsf{DF}^+(S) \in S
insert \phi-function for v at the start of B_n
```

Renaming Variables (Pseudo Code)

- Rename from the Entry node recursively
 - ► For each variable x, maintain a rename stack of x → x_{version} mapping
- For node n
 - For each assignment (x = ...) in n
 - If non-\(\phi\) assignment, rename any use of x with the Top mapping of x from the rename stack
 - Push the mapping $x \mapsto x_i$ on the rename stack
 - Replace lhs of the assignment by x_i
 - i = i + 1
- For the successors of *n*
 - Rename ϕ operands through SUCC edge index
- Recursively rename all child nodes in the dominator tree
- For each assignment (x = ...) in n
 - ▶ Pop $x \mapsto \ldots$ from the rename stack