# CS 335: Semantic Analysis 

Swarnendu Biswas

Department of Computer Science and Engineering, Indian Institute of Technology Kanpur

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An Overview of Compilation


## Beyond Scanning and Parsing

```
int a, b;
a = b + c;
```

```
std::string x;
    int y;
    y = x+3;
```

```
int dot_prod(int x[], int y[]) {
    int d = 0, i;
    for (i=0; i<10; i++)
        d += x[i]*y[i];
    return d;
}
int main() {
    int p, a[10], b[10];
    p = dot_prod(a, b);
    return 0;
}
```

Example static semantic checks that a compiler can perform:

- p , a , and b are declared before use
- Number and type of the parameters of dot_prod() are the same in its declaration and use
- Types of $p$ and return type of dot_prod() match


## Beyond Scanning and Parsing

A compiler must do more than just recognize whether a sentence belongs to a programming language grammar

- An input program can be grammatically correct but may contain other errors that prevent compilation
- Lexer and parser cannot catch all program errors

Some language features cannot be modeled using context-free grammars (CFGs)

- A variable has been declared before use
- Parameter types and numbers match in the declaration and use of a function
- Types match on both sides of an assignment


## Limitations with CFGs

## Ensures variable declarations go before their uses

$$
\text { ProcBody } \rightarrow \text { Decls Executables }
$$

- CFGs only deal with syntactic categories and structure
- Enforcing the "declare before use" rule requires knowledge that cannot be encoded in a CFG
- Grammar can specify the positions in an expression where a variable name may occur, but cannot enforce the "declare before use" rule
- CFG cannot match one instance of a variable name with another
- Programming languages also allow to include declarations within executable statements


## Additional Checks a Compiler Needs to Perform



Compilers need to understand the structure of the computation to translate the input program

## Additional Checks a Compiler Needs to Perform

## Questions

Has a variable been declared?
What is the type and size of a variable?
Is the variable a scalar or an array?
Is an array access A [i] [j] [k] consistent with the declaration?
Does the name x correspond to a variable or a function?
If $x$ is a function, how many arguments does it take?
What kind of value, if any, does a function x return?
Are all invocations of a function consistent with its declaration?
Track inheritance relationship
Ensure that classes and their methods are not multiply-defined

## Semantic Analysis

- Finding answers to these questions is part of the semantic analysis phase
- Static semantics of languages can be checked at compile time
- For example, ensure variable are declared before their uses, check that each expression has a correct type, and programs must have valid locations to transfer the control flow
- Dynamic semantics of languages need to be checked at run time
- Whether an overflow will occur during an arithmetic operation?
- Whether array bounds will be exceeded during execution?
- Whether recursion will exceed stack limits?
- Compilers can generate code to check dynamic semantics


## How Does a Compiler Check Semantics?

- Compilers track additional information for semantic analysis
- For example, types of variables, function parameters, and array dimensions
- Type information is stored in the symbol table or the syntax tree
- The information required may be non-local in some cases
- Semantic analysis can be performed during parsing or in another pass that traverses the IR produced by the parser
- Implementation choices
- Use formal methods like context-sensitive grammars
- Building efficient parsers is challenging
- Use ad-hoc techniques using symbol table
- Static semantics of PL can be specified using attribute grammars
- Attribute grammars are extensions of context-free grammars
- Additional information can be used not only for semantic validation but also during subsequent phases of compilation


## Attribute Grammar Framework

## Syntax-Directed Definition

## Definition

A syntax-directed definition (SDD) is a context-free grammar with attributes and semantic rules to evaluate the attributes

- Attributes may be of any type: numbers, strings, pointers to structures
- Attributes are associated with nodes in the parse tree, and each instance of a grammar symbol in the parse tree has an associated attribute

| Production | Semantic Rule |
| :--- | :--- |
| $E \rightarrow E_{1}+T$ | $E . c o d e=E_{1} . \operatorname{code}\\|T . c o d e\\| \\|^{*}+"$ |

## Attribute grammars are SDDs with no side effects

Help track context-sensitive information via attributes

## Syntax-Directed Definition

- Generalization of CFG where each grammar symbol has an associated set of attributes
- Let $G=(T, N T, S, P)$ be a CFG and let $V=T \cup N T$
- Every symbol $X \in V$ is associated with a set of attributes (e.g., $X$.a and $X . b$ )
- Each attribute takes values from a specified domain (finite or infinite) based on its type
- Typical domains of attributes are, integers, reals, characters, strings, booleans, and structures
- New domains can be constructed from given domains by mathematical operations such as cross product and map
- Values of attributes are computed by semantic rules


## Attribute Grammar for Signed Binary Numbers

Consider a grammar for signed binary numbers


Build an attribute grammar that annotates a number with the value it represents.

Associate attributes with grammar symbols

| Symbol | Attributes |
| :---: | :---: |
| number | val |
| sign | neg |
| list | pos, val |
| bit | pos, val |

## Attribute Grammar for Signed Binary Numbers

| Production | Attribute Rule |
| :---: | :---: |
| number $\rightarrow$ sign list | ```list.pos = 0 if sign.neg: number.val = -list.val else: number.val = list.val``` |
| sign $\rightarrow+$ | sign.neg = false |
| sign $\rightarrow$ | sign.neg = true |
| list $\rightarrow$ bit | bit.pos = list.pos <br> list.val = bit.val |
| list $\rightarrow$ list ${ }_{1}$ bit | $\begin{aligned} & \text { list }_{1} . \text { pos }=\text { list.pos }+1 \\ & \text { bit.pos }=\text { list } . p o s ~_{\text {list.val }=\text { list }_{1} . v a l+\text { bit.val }}^{\text {lol }} \end{aligned}$ |
| bit $\rightarrow 0$ | bit.val $=0$ |
| bit $\rightarrow 1$ | bit.val $=2^{\text {bit.pos }}$ |



## Annotated Parse Tree for -101

## Definition

A parse tree showing the value(s) of its attribute(s) is called an annotated parse tree


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## Types of Nonterminal Attributes

## Synthesized

- Value of a synthesized attribute for a nonterminal $A$ at a node $N$ is computed from the values of children nodes and $N$ itself (e.g., code and neg)
- Defined by a semantic rule associated with a production at $N$ such that the production has $A$ as its head


## Inherited

- Value of an inherited attribute for a nonterminal $B$ at a node $N$ is computed from the values at $N$ 's parent, $N$ itself, and $N$ 's siblings (e.g., pos)
- Defined by a semantic rule associated with the production at the parent of $N$ such that the production has $B$ in its body


## Understanding Synthesized and Inherited Attributes

- Suppose a grammar production $A \rightarrow \alpha$ has an associated semantic rule $b=f\left(c_{1}, c_{2}, \ldots c_{k}\right)$
(i) If $b$ is a synthesized attribute of $A$, then $c_{1}, c_{2}, \ldots c_{k}$ are attributes of symbols in the production
(ii) If $b$ is an inherited attribute of a symbol in the body, then $c_{1}, c_{2}, \ldots c_{k}$ are attributes of symbols in the production
- Start symbol cannot have inherited attributes
- Terminals can have synthesized attributes, but not inherited attributes
- Attributes for terminals have lexical values that are supplied by the lexical analyzer


## Dependency Graph

- If an attribute $b$ depends on an attribute $c$, then the semantic rule for $b$ must be evaluated after the semantic rule for $c$
- The dependencies among the nodes are depicted by a directed graph called the dependency graph
- Annotated parse tree shows the values at attributes, while the dependency graph shows how the values need to be computed


## Dependency Graph

- Suppose A.a $=f(X . x, Y . y)$ is a semantic rule for $A \rightarrow X Y$


Parse
Dependency
tree

- Suppose $X . x=f(A . a, Y . y)$ is a semantic rule for $A \rightarrow X Y$


Parse tree


Dependency graph

## Construct Dependency Graph

```
for each node n in the parse tree do
    for each attribute a of the grammar symbol }n\mathrm{ do
        construct a node in the dependency graph for a
for each node n in the parse tree do
    for each semantic rule b=f(c, c, c,.., ck) do
        // Rule is associated with production at node n
        for i = 1 to k do
            construct an edge from ci to b
```


## Example of a Dependency Graph



## Evaluating an SDD

## In what order do we evaluate attributes in an implementation?

- We must evaluate all the attributes upon which the attribute of a node depends
- SDDs do not specify any order of evaluation
- For SDDs with both synthesized and inherited attributes, there is no guarantee of an order of evaluation existing

A compiler must deal with circularity appropriately for attribute grammars

## Production Semantic Rules

$$
\begin{array}{ll}
A \rightarrow B & \text { A.s }=B . i \\
B . i=A . s+1
\end{array}
$$



## Evaluating an SDD

Parse tree method

- In the absence of cycles, topologically sort the dependency graph to find the evaluation order
- Any topological sort of dependency graph gives a valid partial order in which semantic rules must be evaluated
- Each rule executes as soon as all its input operands are available

Rule-based method

- Semantic rules are analyzed and the order of evaluation is predetermined
- E.g., evaluate list.pos first and list.val later in slide 14

Oblivious method Evaluation order ignores the semantic rules, and makes repeated left-to-right and right-to-left passes until all attributes have values

## Types of SDDs

- Cycles should be avoided since the compiler can no longer meaningfully proceed with evaluation
- Expensive to identify whether an arbitrary SDD will have cycles
- S-attributed and L-attributed SDDs guarantee no cycles by definition


## S-Attributed Definition

- An SDD that involves only synthesized attributes is called S-attributed definition
- Each rule computes an attribute for the head nonterminal from attributes taken from the body of the production
- Semantic rules in an S-attributed definition can be evaluated by a bottom-up or postorder traversal of the parse tree
- An S-attributed SDD can be implemented naturally in conjunction with an LR parser

```
postorder(N) {
    for (each child C of N, from left to right)
        postorder(C)
    evaluate the attributes associated with node N
}
```


## Example of S-Attributed Definition

| Production | Semantic Rules |
| :--- | :--- |
| $L \rightarrow E \$$ | L.val $=E . v a l$ |
| $E \rightarrow E_{1}+T$ | E.val $=E_{1}$. val $+T . v a l$ |
| $E \rightarrow T$ | $E . v a l=T . v a l$ |
| $T \rightarrow T_{1} * F$ | $T . v a l=T_{1} . v a l \times F . v a l$ |
| $T \rightarrow F$ | $T . v a l=F . v a l$ |
| $F \rightarrow(E)$ | F.val $=E . v a l$ |
| $F \rightarrow$ digit | F.val $=$ digit.lexval |



Annotated Parse Tree for $3 * 5+4 \$$


## Abstract Syntax Tree (AST)

## Definition

An AST is a condensed form of a parse tree that is used for representing language constructs

- Each leaf is an operand and non-leaf nodes represent operators
- ASTs represent relationships between language constructs, do not bother with derivations

$$
S \rightarrow \text { if } P \text { then } S_{1} \text { else } S_{2}
$$



Parse trees are also called concrete syntax trees

## Parse Tree vs Abstract Syntax Tree

## Parse Tree



Abstract Syntax Tree


## Inherited Attributes

Useful when the structure of the parse tree does not match the abstract syntax of the source code

| Production | Semantic Rules |
| :--- | :--- |
| $T \rightarrow F T^{\prime}$ | $T^{\prime}$. inh $=F$. val |
|  | $T_{1}^{\prime} . v a l=T^{\prime}$. syn |
| $T^{\prime} \rightarrow * F T_{1}^{\prime}$ | $T_{1}^{\prime}$.inh $=T^{\prime}$. inh $\times F$. .val |
| $T^{\prime}$. syn $=T_{1}^{\prime}$. syn |  |
| $T^{\prime} \rightarrow \epsilon$ | $T^{\prime}$. syn $=T^{\prime}$. inh |
| $F \rightarrow$ digit | F.val $=$ digit.lexval |

## Parse Tree, AST, and Annotated Parse Tree for $3 * 5$



## Example SDD with Side Effects

| Production | Semantic Rules |
| :--- | :--- |
| $D \rightarrow T L$ | L.inh = T.type |
| $T \rightarrow$ float | T.type $=$ float |
| $T \rightarrow$ int | T.type $=$ int |
| $L \rightarrow L_{1}$, id | $L_{1}$.inh $=$ L.inh; addtype(id.entry, L.inh) |
| $L \rightarrow$ id | addtype(id.entry, L.inh $)$ |

addtype() sets L.in as the type of the symbol table object pointed to by id.entry (implies a side effect).

Annotated Parse Tree for float $x, y, z$


## Notes about Inherited Attributes

- Always possible to rewrite an SDD to use only synthesized attributes
- Inherited attributes can be simulated with synthesized attributes and helper functions
- May be more logical to use both synthesized and inherited attributes
- Inherited attributes usually cannot be evaluated by a simple preorder traversal of the parse tree
- Attributes may depend on both left and right siblings!
- Attributes that do not depend on right children can be evaluated by a preorder traversal


## Bottom-up Evaluation of S-Attributed Definitions

- Suppose $A \rightarrow X Y Z$, and the semantic rule is $A=f(X . x, Y . y, Z . z)$
- Attributes can be computed during bottom-up parsing
- Extend the stack to hold values
- On reduction, value of new synthesized attribute $A . a$ is computed from the attributes on the stack



## Example S-Attributed Definition

| Production | Semantic Rules |
| :--- | :--- |
| $L \rightarrow E \$$ | L.val $=E . v a l$ |
| $E \rightarrow E_{1}+T$ | $E . v a l=E_{1}$. val $+T . v a l$ |
| $E \rightarrow T$ | E.val $=T . v a l$ |
| $T \rightarrow T_{1} * F$ | $T . v a l=T_{1} . v a l \times F . v a l$ |
| $T \rightarrow F$ | $T . v a l=F . v a l$ |
| $F \rightarrow(E)$ | F.val $=E . v a l$ |
| $F \rightarrow$ digit | F.val $=$ digit.lexval |

## Bottom-up Evaluation of S-Attributed Definition

| Value | Stack | Input | Action |
| :--- | :--- | ---: | :--- |
| $\$$ | $\$$ | $3 * 5+4 \$$ | Shift 3 |
| $\$ 3$ | $\$$ digit | $* 5+4 \$$ | Reduce by $F \rightarrow$ digit |
| $\$ 3$ | $\$ F$ | $* 5+4 \$$ | Reduce by $T \rightarrow F$ |
| $\$ 3$ | $\$ T$ | $* 5+4 \$$ | Shift $*$ |
| $\$ 3$ | $\$ T *$ | $5+4 \$$ | Shift $*$ |
| $\$ 35$ | $\$ T *$ digit | $+4 \$$ | Reduce by $F \rightarrow$ digit |
| $\$ 35$ | $\$ T * F$ | $+4 \$$ | Reduce by $T \rightarrow T * F$ |
| $\$ 15$ | $\$ T$ | $+4 \$$ | Reduce by $E \rightarrow T$ |
| $\$ 15$ | $\$ E$ | $+4 \$$ | Shift + |
| $\$ 15$ | $\$ E+$ | $4 \$$ | Shift 4 |
| $\$ 154$ | $\$ E+$ digit | $\$$ | Reduce by $F \rightarrow$ digit |
| $\$ 154$ | $\$ E+F$ | $\$$ | Reduce by $T \rightarrow F$ |
| $\$ 154$ | $\$ E+T$ | $\$$ | Reduce by $E \rightarrow E+T$ |
| $\$ 19$ | $\$ E$ | $\$$ | Accept |

## L-Attributed Definitions

- Each attribute must be either
(i) Synthesized, or
(ii) Suppose $A \rightarrow X_{1} X_{2} \ldots X_{n}$ and $X_{i}$.a is an inherited attribute. $X_{i}$.a can be computed using
(a) Only inherited attributes from $A$, or
(b) Either inherited or synthesized attributes associated with $X_{1}, \ldots, X_{i-1}$, or
(c) Inherited or synthesized attributes associated with $X_{i}$.
- Dependences flow from left-to-right among inherited attributes


## Production Semantic Rule

| $T \rightarrow F T^{\prime}$ | $T^{\prime}$. inh $=F$. val |
| :--- | :--- |
|  | $T . v a l=T^{\prime}$. syn |
| $T^{\prime} \rightarrow * F T_{1}^{\prime}$ | $T_{1}^{\prime}$ inh $=T^{\prime}$. inh $\times F$. val |
| $T_{1}^{\prime}$. syn $=T_{1}^{\prime}$ syn |  |
| $T^{\prime} \rightarrow \epsilon$ | $T^{\prime}$. syn $=T^{\prime}$. inh |
| $F \rightarrow$ digit | F.val $=$ digit.lexval |

## Are these SDDs S- or L-attributed?

| Production | Semantic Rule |
| :--- | :--- |
| $A \rightarrow B C$ | $A . a=B . b_{1}$ <br> $B . b_{2}=f(A . a, C . c)$ |
|  | Semantic Rule |
| $A \rightarrow B C$ | $B . i=f_{1}(A . i)$ <br> $C . i=f_{2}(B . s)$ <br> $A . s=f_{3}(C . s)$ |
| Production | Semantic Rule |
|  | $C . i=f_{4}(A . i)$ <br> $A \rightarrow B C$ |
|  | $A . i=f_{5}(C . s)$ |
|  |  |

## S-Attributed and L-Attributed Definitions

Every S-attributed grammar is also a L-attributed grammar

All L-attributed grammars are not S -attributed

## Summarizing Attribute Grammars

- Attribute grammars define a set of attributes and translations at every node of the parse tree, the output is available at the root
- Functional style which hides implementation details
- Evaluation order is not specified among multiple attributes for a production
- Only requirement is there should not be any circularity


## Challenges with Attribute Grammars

- Rules only involve local information (i.e., attributes pertaining to symbols in the production)
- Needs additional attributes and copy rules to use non-local information, which increases memory and run-time overhead
- Results can be scattered across attributes in the parse tree
- Moving important attributes to the root node introduces additional copy instructions
- Works in conjunction with a parse tree or an AST, but a compiler implementation may not build either


## Syntax-Directed Translation

## Syntax-Directed Translation (SDT)

- Program fragments are embedded as semantic actions in the production body of a CFG
- Generates code while parsing
- Indicates the order in which semantic actions are to be evaluated

$$
\text { rest } \rightarrow+\text { term }\left\{\operatorname { p r i n t } \left({ }^{\prime}+\text { ') \} rest }{ }_{1}\right.\right.
$$

- Executable specification of an SDD, is easier to implement, and can be more efficient since the compiler can avoid constructing a parse tree and a dependency graph
- E.g., Bison uses translation schemes


## SDD for Infix to Postfix Translation

- Postfix notation for an expression $E$ is defined inductively
- If $E$ is a variable or constant, then postfix notation is $E$
- If $E=E_{1}$ op $E_{2}$ where op is any binary operator, then the postfix notation is $E_{1}^{\prime} E_{2}^{\prime}$ op, where $E_{1}^{\prime}$ and $E_{2}^{\prime}$ are postfix notations for $E_{1}$ and $E_{2}$ respectively
- If $E=\left(E_{1}\right)$, then postfix notation for $E_{1}$ is the postfix notation for $E$


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- If $E=\left(E_{1}\right)$, then postfix notation for $E_{1}$ is the postfix notation for $E$

| Production | Semantic Rules |
| :--- | :--- |
| expr $\rightarrow$ expr $_{1}+$ term | expr.code $=$ expr $_{1} . c o d e \\|$ term.code $\\| "+"$ |
| expr $\rightarrow$ expr $r_{1}-$ term | expr.code $=$ expr ${ }_{1} . c o d e \\|$ term.code $\\| "-"$ |
| expr $\rightarrow$ term | expr.code $=$ term.code |
|  | term.code $=" 0 "$ |
| term $\rightarrow 0\|1\| \ldots \mid 9$ | term.code $=" 1 "$ |
|  | $\ldots$ |
|  | term.code $=" 9 "$ |

## SDT for Infix to Postfix Translation

 SDD| Production | Semantic Rules |
| :--- | :--- |
| expr $\rightarrow$ expr $_{1}+$ term | expr.code $=$ expr $_{1} . c o d e\\|t e r m . c o d e\\| "+"$ |
| expr $\rightarrow$ expr $r_{1}-$ term | expr.code $=$ expr $r_{1} . c o d e \\| t e r m . c o d e\| \| "-"$ |
| expr $\rightarrow$ term | expr.code $=$ term.code |
|  | term.code $=" 0 "$ |
| term $\rightarrow 0\|1\| \ldots \mid 9$ | term.code $=" 1 "$ |
|  | $\ldots$ |
|  | term.code $=" 9 "$ |


| Production | Semantic Actions |
| :---: | :---: |
| expr $\rightarrow$ expr ${ }_{1}+$ term | \{print("+")\} |
| expr $\rightarrow$ expr ${ }_{1}$ - term | \{print(" - ") \} |
| expr $\rightarrow$ term |  |
|  | \{print("0")\} |
| term $\rightarrow$ 0\|1| 19 | \{print("1")\} |
|  | $\text { \{print("9")\} }$ |

## SDT Actions to Translate $9-5+2$ to Postfix



## Construction of AST for Expressions

- Idea: Construct subtrees for subexpressions by creating an operator and operand nodes
- Helper functions
(i) Create an internal node with label op and $k$ fields denoting $k$ children with $\operatorname{Node}\left(o p, c_{1}, c_{2}, \ldots, c_{k}\right)$
(ii) Create a leaf node with label op and val as the lexical value with $\operatorname{Leaf}(o p, v a l)$
- The following sequence of function calls creates an AST for $a-4+c$

1. $p_{1}=$ new $\operatorname{Leaf}\left(\mathbf{i d}\right.$, entry $\left.{ }_{a}\right)$
2. $p_{2}=$ new $\operatorname{Leaf}($ num, 4$)$

3. $p_{3}=$ new Node(" - ", $p_{1}, p_{2}$ )
4. $p_{4}=$ new $\operatorname{Leaf}\left(\mathbf{i d}\right.$, entry $\left.{ }_{c}\right)$
5. $p_{5}=$ new Node(" + ", $p_{3}, p_{4}$ )

## S-Attributed Definition for Constructing ASTs

| Production | Semantic Actions |
| :--- | :--- |
| $E \rightarrow E_{1}+T$ | $E . n o d e=$ new $\operatorname{Node}\left("+", E_{1}\right.$. node, $\left.T . n o d e\right)$ |
| $E \rightarrow E_{1}-T$ | $E . n o d e=$ new $\operatorname{Node}\left("-", E_{1}\right.$. node,$\left.T . n o d e\right)$ |
| $E \rightarrow T$ | $E . n o d e=T . n o d e$ |
| $T \rightarrow(E)$ | $T . n o d e=E . n o d e$ |
| $T \rightarrow$ id | $T . n o d e=$ new $\operatorname{Leaf}\left(\right.$ id, entry $\left.y_{i d}\right)$ |
| $T \rightarrow$ num | $T . n o d e=$ new $\operatorname{Leaf}($ num, num.$v a l)$ |

Construction of AST for $a-4+c$


Construction of AST for $a-4+c$


## L-Attributed Definition for Constructing Syntax Trees

## Production Semantic Actions

$$
\begin{aligned}
& E \rightarrow T E^{\prime} \quad E . n o d e=E^{\prime} . \text { syn } \\
& E^{\prime}=T \text {.node } \\
& \left.E^{\prime} \rightarrow+T E_{1}^{\prime} \quad E_{1}^{\prime} \text {.inh }=\text { new Node(" }+ \text { ", } E^{\prime} \text {.inh, } T \text {.node }\right) \\
& E^{\prime} \rightarrow-T E_{1}^{\prime} \quad E_{1}^{\prime} \text {. inh }=\text { new Node(" - ", } E^{\prime} \text {.inh, T.node) } \\
& E^{\prime} . \text { syn }=E_{1}^{\prime} \text {.syn } \\
& E^{\prime} \rightarrow \epsilon \quad E^{\prime} . \text { syn }=E^{\prime} . \text { inh } \\
& T \rightarrow(E) \quad \text { T.node }=E \text {.node } \\
& T \rightarrow \mathbf{i d} \quad \text { T.node }=\text { new } \operatorname{Leaf}\left(\mathbf{i d}, \text { entry }{ }_{\text {id }}\right) \\
& T \rightarrow \text { num } \quad T . n o d e=\text { new } \operatorname{Leaf}(\text { num, num.val) }
\end{aligned}
$$

## Dependency Graph for $a-4+c$



## Implementing SDTs

- Any SDT can be implemented by
(i) building a parse tree, and
(ii) performing the actions in a left-to-right depth-first order (i.e., preorder traversal)
- Need to make all attribute values available when the semantic action is executed
- SDTs are often implemented during parsing, possibly without a parse tree, provided
- Underlying grammar is LR and the SDD is S-attributed, or
- Underlying grammar is LL and the SDD is L-attributed
- When semantic action involves only synthesized attributes, the action can be put at the end of the production
- SDT with all actions at the right end of a production is called postfix SDT


## Postfix SDT for the Desk Calculator

- Consider S-attributed SDD for a bottom-up grammar
- We can construct an SDT with actions at the end of each production

| $L \rightarrow E \$$ | \{print $(E . v a l)\}$ |
| :--- | :--- |
| $E \rightarrow E_{1}+T$ | $E . v a l=E_{1} . v a l+T . v a l$ |
| $E \rightarrow T$ | $E . v a l=T . v a l$ |
| $T \rightarrow T_{1} * F$ | T.val $=T_{1} . v a l \times F . v a l$ |
| $T \rightarrow F$ | T.val $=$ F.val |
| $F \rightarrow(E)$ | F.val $=$ E.val |
| $F \rightarrow$ digit | F.val $=$ digit.val |
|  |  |

## Implementing Postfix SDTs During LR Parsing



- Use a value stack to maintain attributes along with the states (grammar symbols)
- Execute actions when reductions take place
- Manipulating the stack is done by the LR parser


## Implementing Postfix SDTs with Bottom-up Parsing

## Production Semantic Actions

$$
\begin{array}{ll}
L \rightarrow E \$ & \text { \{print(stack[top - 1].val); top = top }-1 ;\} \\
\hline E \rightarrow E_{1}+T & \begin{array}{l}
\text { \{stack[top }-2] . v a l=\text { stack[top }-2] . v a l+\text { stack[top].val; } \\
\\
\text { top = top }-2 ;\}
\end{array}
\end{array}
$$

$$
E \rightarrow T
$$

$$
\begin{aligned}
T \rightarrow T_{1} * F & \begin{array}{l}
\text { \{stack[top }-2] . v a l=\text { stack[top }-2] . v a l \times \text { stack[top].val; } \\
\\
\text { top }=\text { top }-2 ;\}
\end{array}
\end{aligned}
$$

$$
T \rightarrow F
$$

$$
F \rightarrow(E) \quad\{\text { stack[top }-2] . \mathrm{val}=\text { stack[top }-1] . \mathrm{val} ; \text { top }=\text { top }-2 ;\}
$$

$$
F \rightarrow \text { digit }
$$

## SDT with Actions Inside Productions

$$
B \rightarrow X\{a\} Y
$$

- For top-down parsing, execute action a just before expanding nonterminal $Y$ or checking for terminal $Y$ in the input
- For bottom-up parsing, execute action a as soon as $X$ occurs on top of the stack


## Infix-to-Prefix SDT Problematic for Translating During Parsing

$$
\begin{aligned}
& L \rightarrow E \$ \\
& E \rightarrow\{\operatorname{print}("+")\} E_{1}+T \\
& E \rightarrow T \\
& T \rightarrow\{\operatorname{print}(" * ")\} T_{1} * F \\
& T \rightarrow F \\
& F \rightarrow(E) \\
& F \rightarrow \operatorname{digit}\{\text { print(digit.lexval) }\}
\end{aligned}
$$

Needs to print even before seeing what is there next in the input

## Implementing SDTs with Embedded Actions

(i) Parse the input and produce a parse tree (ignore semantic actions)
(ii) Examine each interior node $N$ for production $A \rightarrow \alpha$

- Add additional children to $N$ for the actions in $\alpha$, in left-to-right order
(iii) Perform a preorder traversal of the tree and execute the action when a node labeled by an action is visited



## Converting L-attributed SDDs to SDTs

- An inherited attribute for a nonterminal $A$ in the body of a production must be computed in an action before the occurrence of $A$ in the body
- A synthesized attribute for the nonterminal on the LHS can only be computed when all the attributes it references in the body have been computed
- The action is usually put at the end of the production

$$
S \rightarrow \text { while }(C) S_{1}
$$

| Symbol | Attributes |
| :---: | :---: |
| S | next, code |
| C | true, false, code |

S.code and C.code are synthesized attributes, while S.next, C.true, and C.false are inherited attributes

## Example of Converting L-attributed SDDs to SDTs

## SDD

| Production | Semantic Rules |
| :---: | :---: |
| $S \rightarrow$ while (C) $S_{1}$ | ```L1 = new Label(); L2 = new Label(); C.false = S.next; C.true = L2; S1.next = L1; S.code = label\||L1||C.code||label||2||S .code``` |

SDT

$$
\begin{array}{cl}
S \rightarrow \text { while }( & \{L 1=\text { new Label }() ; L 2=\text { new Label }() ; \\
C) & C . f a l s e=\text { S.next } ; C . \text { true }=L 2 ;\} \\
S_{1} & \left\{S_{1} . \text { next }=L 1 ;\right\} \\
& \left\{S . \text { code }=\text { label }\|L 1\| C . \text { code } \| \text { label }\|L 2\| S_{1} . \text { code } ;\right\} \\
\hline
\end{array}
$$

## References

A. Aho et al. Compilers: Principles, Techniques, and Tools. Sections 2.3, 5.1-5.4, 2 ${ }^{\text {nd }}$ edition, Pearson Education.
K. Cooper and L. Torczon. Engineering a Compiler. Sections 4.1, 4.3-4.4, $2^{\text {nd }}$ edition, Morgan Kaufmann.

