# CS 335: Semantic Analysis 

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## An Overview of Compilation



## Beyond Scanning and Parsing

```
int a, b;
a = b + c;
```

std::string $x ;$
int $y$;
$y=x+3 ;$

```
int dot_prod(int x[], int y[]) {
    int d, i;
    d = 0;
    for (i=0; i<10; i++)
        d += x[i]*y[i];
    return d;
int main() {
    int p, a[10], b[10];
    p = dot_prod(a, b);
    return 0;
}
```


## Beyond Scanning and Parsing

- A compiler must do more than just recognize whether a sentence belongs to a programming language grammar
- An input program can be grammatically correct but may contain other errors that prevent compilation
- Lexer and parser cannot catch all program errors
- Some language features cannot be modeled using context-free grammar (CFG)
- Whether a variable has been declared before use?
- Parameter types and numbers match in the declaration and use of a function
- Types match on both sides of an assignment


## Limitations with CFGs

## ProcedureBody $\rightarrow$ Declarations Executables <br> Ensures variable declarations go before their uses

- CFGs only deal with syntactic categories and structure
- Enforcing the "declare before use" rule requires knowledge that cannot be encoded in a CFG
- Grammar can specify the positions in an expression where a variable name may occur, but can enforce the "declare before use" rule
- CFG cannot match one instance of a variable name with another
- Programming languages also allow to include declarations within executable statements


## Questions That Compiler Needs to Answer



## Questions That Compiler Needs to Answer



Compilers need to understand the structure of the computation to translate the input program

## Semantic Analysis

- Finding answers to these questions is part of the semantic analysis phase
- Static semantics of languages can be checked at compile time
- For example, ensure variable are declared before their uses, check that each expression has a correct type, and programs must have valid locations to transfer the control flow.


## Checking Dynamic Semantics

- Dynamic semantics of languages need to be checked at run time
- Whether an overflow will occur during an arithmetic operation?
- Whether array bounds will be exceeded during execution?
- Whether recursion will exceed stack limits?
- Compilers can generate code to check dynamic semantics

```
int dot_prod(int x[], int y[]) {
    int d, i;
    d = 0;
    for (i=0; i<10; i++)
        d += x[i]*y[i];
    return d;
}
int main() {
    int p; int a[10], b[10];
    p = dot_prod(a, b);
    return 0;
}
```


## How does a compiler answer these questions?

- Compilers track additional information for semantic analysis
- For example, types of variables, function parameters, and array dimensions
- Type information is stored in the symbol table or the syntax tree
- Used not only for semantic validation but also for subsequent phases of compilation
- The information required may be non-local in some cases
- Semantic analysis can be performed during parsing or in another pass that traverses the IR produced by the parser


## How does a compiler answer these questions?

- Use formal methods like context-sensitive grammars
- Building efficient parsers is challenging
- Use ad-hoc techniques using symbol table
- Static semantics of PL can be specified using attribute grammars
- Attribute grammars are extensions of context-free grammars

Attribute Grammar Framework

## Syntax-Directed Definition

- A syntax-directed definition (SDD) is a context-free grammar with attributes and semantic rules to evaluate the attributes
- Attributes may be of any type: numbers, strings, pointers to structures
- Attributes are associated with nodes in the parse tree, and each instance of a grammar symbol in the parse tree has an associated attribute

| Production | Semantic Rule |
| :---: | :---: |
| $E \rightarrow E_{1}+T$ | $E . \operatorname{code}=E_{1} \cdot \operatorname{code}\\|T \cdot \operatorname{code}\\| "+{ }^{\prime}{ }^{\prime}$ |

- Attribute grammars are SDDs with no side effects
- Help track context-sensitive information via attributes


## Syntax-Directed Definition

- Generalization of CFG where each grammar symbol has an associated set of attributes
- Let $G=(T, N T, S, P)$ be a CFG and let $V=T \cup N T$
- Every symbol $X \in V$ is associated with a set of attributes (e.g., $X . a$ and $X . b$ )
- Each attribute takes values from a specified domain (finite or infinite), which is its type
- Typical domains of attributes are, integers, reals, characters, strings, booleans, and structures
- New domains can be constructed from given domains by mathematical operations such as cross product and map
- Values of attributes are computed by semantic rules


## Attribute Grammar for Signed Binary Numbers

Consider a grammar for signed binary numbers
number $\rightarrow$ sign list
sign $\rightarrow+\mid-$
list $\rightarrow$ list bit $\mid$ bit
bit $\rightarrow 0 \mid 1$
Build an attribute grammar that annotates number with the value it represents

Associate attributes with grammar symbols

| Symbol | Attributes |
| :---: | :---: |
| number | val |
| sign | neg |
| list | pos,val |
| bit | pos,val |

## Attribute Grammar for Signed Binary Numbers

| Production | Attribute Rule |
| :---: | :---: |
| number $\rightarrow$ sign list | ```list.pos \(=0\) if sign.neg: number.val \(=-l i s t . v a l\) else: number.val \(=-l i s t . v a l\)``` |
| $\operatorname{sign} \rightarrow+$ | sign. $n$ eg $=$ false |
| sign $\rightarrow$ - | sign. $n$ eg = true |
| list $\rightarrow$ bit | $\begin{aligned} & \text { bit. } . \text { os }=\text { list.pos } \\ & \text { list.val }=\text { bit.val } \end{aligned}$ |
| list ${ }_{0} \rightarrow$ list $_{1}$ bit | $\begin{aligned} & \text { list }_{1} \cdot \text { pos }=\text { list }_{0} \cdot \text { pos }+1 \\ & {\text { bit.pos }=\text { list }_{0} \cdot p o s}_{\text {list }_{0} \cdot v a l=\text { list }_{1} \cdot v a l+\text { bit.val }}=\text {.val } \end{aligned}$ |
| bit $\rightarrow 0$ | bit.val $=0$ |
| bit $\rightarrow 1$ | bit.val $=2^{\text {bit.pos }}$ |

## Parse Tree for -101



## Annotated Parse Tree for -101

- A parse tree showing the value(s) of its attribute(s) is called an annotated parse tree



## Annotated Parse Tree for -101

val =?

- A parse tree showing the value(s) of its attribute(s) is called an annotated parse tree



## Annotated Parse Tree for -101

- A parse tree showing the value(s) of its attribute(s) is called an annotated parse tree



## Types of Nonterminal Attributes

## Synthesized

- Value of a synthesized attribute for a nonterminal $A$ at a node $N$ is computed from the values of children nodes and $N$ itself (e.g., val and neg)
- Defined by a semantic rule associated with a production at $N$ such that the production has $A$ as its head


## Inherited

- Value of an inherited attribute for a nonterminal $B$ at a node $N$ is computed from the values at $\boldsymbol{N}$ 's parent, $\boldsymbol{N}$ itself, and $\boldsymbol{N}$ 's siblings (e.g., pos)
- Defined by a semantic rule associated with the production at the parent of $N$ such that the production has $B$ in its body


## Syntax-Directed Definition

- A grammar production $A \rightarrow \alpha$ has an associated semantic rule $b=$ $f\left(c_{1}, c_{2}, \ldots, c_{k}\right)$
- $b$ is a synthesized attribute of $A$ and $c_{1}, c_{2}, \ldots, c_{k}$ are attributes of symbols in the production
- $b$ is an inherited attribute of a symbol in the body, and $c_{1}, c_{2}, \ldots, c_{k}$ are attributes of symbols in the production
- Start symbol cannot have inherited attributes
- Terminals can have synthesized attributes, but not inherited attributes
- Attributes for terminals have lexical values that are supplied by the lexical analyzer


## Dependency Graph

- If an attribute $b$ depends on an attribute $c$ then the semantic rule for $b$ must be evaluated after the semantic rule for $c$
- The dependencies among the nodes are depicted by a directed graph called dependency graph
- Annotated parse tree shows the values at attributes, while the dependency graph shows how the values need to be computed


## Dependency Graph

- Suppose A. $a=f(X . x, Y . y)$ is a semantic rule for $A \rightarrow X Y$

- Suppose $X . x=f(A . a, Y . y)$ is a semantic rule for $A \rightarrow X Y$



## Construct Dependency Graph

for each node $n$ in the parse tree do
for each attribute $a$ of the grammar symbol do
construct a node in the dependency graph for $a$
for each node $n$ in the parse tree do
for each semantic rule $b=f\left(c_{1}, c_{2}, \ldots, c_{k}\right)$ do // Associated with production at node $n$ for $i=1$ to $k$ do
construct an edge from $c_{i}$ to $b$

## Example of a Dependence Graph



## Evaluating an SDD

- In what order do we evaluate attributes in an implementation?
- SDDs do not specify any order of evaluation
- We must evaluate all the attributes upon which the attribute of a node depends
- For SDD's with both synthesized and inherited attributes, there is no guarantee of an order of evaluation existing


## Circular Dependency of Attributes

A compiler must deal with circularity appropriately for attribute grammars


## Evaluating an SDD

- Parse tree method
- In the absence of cycles, use topological sort of the dependency graph to find the evaluation order
- Any topological sort of dependency graph gives a valid partial order in which semantic rules must be evaluated
- Each rule executes as soon as all its input operands are available
- Rule-based method
- Semantic rules are analyzed and order of evaluation is predetermined
- E.g., evaluate list. pos first and list. val later
- Oblivious method
- Evaluation order ignores the semantic rules, makes repeated left-to-right and right-to-left passes until all attributes have values


## Postfix Notation

- Postfix notation for an expression $E$ is defined inductively
- If $E$ is a variable or constant, then postfix notation is $E$
- If $E=E_{1} \mathrm{op} E_{2}$ where op is any binary operator, then the postfix notation is $E_{1}^{\prime} E_{2}^{\prime} \mathrm{op}$, where $E_{1}^{\prime}$ and $E_{2}^{\prime}$ are postfix notations for $E_{1}$ and $E_{2}$ respectively
- If $E=\left(E_{1}\right)$, then postfix notation for $E_{1}$ is the notation for $E$


## SDD for Infix to Postfix Translation

| Production | Semantic Rules |
| :---: | :---: |
| expr $\rightarrow$ expr ${ }_{1}+$ term | expr.code $=$ expr $_{1} \cdot$ code $\\|$ term. code\\| $\mid$ "+" |
| expr $\rightarrow$ expr ${ }_{1}$ - term | expr.code $=$ expr $_{1} . \operatorname{code\\| } \\|$ term.code\\||" ${ }^{\text {- }}$ |
| expr $\rightarrow$ term | expr.code $=$ term. code |
| term $\rightarrow 0\|1\| \ldots \mid 9$ | $\begin{aligned} & \text { term. } \operatorname{code}=" 0 " \\ & \text { term. code }=" 1 " \\ & \ldots \\ & \text { term. code }=" 9 " \end{aligned}$ |

## Annotated Parse Tree



## Types of SDDs

- Cycles need to be avoided since the compiler can no longer meaningfully proceed with evaluation
- Expensive to identify whether an arbitrary SDD will have cycles
- S-attributed and L-attributed SDDs guarantee no cycles


## S-Attributed Definition

- An SDD that involves only synthesized attributes is called S-attributed definition
- Each rule computes an attribute for the head nonterminal from attributes taken from the body of the production
- Semantic rules in a S-attributed definition can be evaluated by a bottom-up or postorder traversal of the parse tree
- An S-attributed SDD can be implemented naturally in conjunction with an LR parser

```
postorder(N) {
    for (each child C of N, from left to right)
        postorder(C)
    evaluate the attributes associated with node N
}
```


## Example of S-Attributed Definition

| Production | Semantic Rules |
| :---: | :--- |
| $L \rightarrow E \$$ | L.val $=E . v a l$ |
| $E \rightarrow E_{1}+T$ | $E . v a l=E_{1} . v a l+T . v a l$ |
| $E \rightarrow T$ | $E . v a l=T . v a l$ |
| $T \rightarrow T_{1} * F$ | $T . v a l=T_{1} . v a l \times F . v a l$ |
| $T \rightarrow F$ | $T . v a l=F . v a l$ |
| $F \rightarrow(E)$ | F.val $=E . v a l$ |
| $F \rightarrow$ digit | F.val $=$ digit. lexval |

## Annotated Parse Tree for $3 * 5+4 \$$



## Abstract Syntax Tree (AST)

- Condensed form of a parse tree used for representing language constructs
- Each leaf is an operand and non-leaf nodes represent operators
- ASTs do not check for string membership in the language for a grammar
- ASTs represent relationships between language constructs, do not bother with derivations

$$
S \rightarrow \text { if } P \text { then } S_{1} \text { else } S_{2}
$$



- Parse trees are also called concrete syntax trees


## Parse Tree vs Abstract Syntax Tree

Parse Tree



Abstract Syntax Tree


## Inherited Attributes

- Useful when the structure of the parse tree does not match the abstract syntax of the source code

| Production | Semantic Rules |
| :---: | :---: |
| $T \rightarrow F T^{\prime}$ | $\begin{aligned} & T^{\prime} \cdot i n h=F \cdot v a l \\ & T . v a l=T^{\prime} . s y n \end{aligned}$ |
| $T^{\prime} \rightarrow * F T_{1}^{\prime}$ | $\begin{aligned} & T_{1}^{\prime} \cdot i n h=T^{\prime} \cdot i n h \times F \cdot v a l \\ & T^{\prime} \cdot \operatorname{syn}=T_{1}^{\prime} \cdot \operatorname{syn} \end{aligned}$ |
| $T^{\prime} \rightarrow \epsilon$ | $T^{\prime}$. syn $=T^{\prime} . \mathrm{inh}$ |
| $F \rightarrow$ digit | F.val $=$ digit. lexval |

## Parse Tree and Annotated Parse Tree for $3 * 5$



## Parse Tree and Annotated Parse Tree for $3 * 5$



## Another Example

## Parse Tree for "float $x, y, z$ "

| Production | Semantic Rules |
| :---: | :--- |
| $D \rightarrow T L$ | L.in $=$ T.type |
| $T \rightarrow$ float | T.type $=$ float |
| $T \rightarrow$ int | T.type $=$ int |
| $L \rightarrow L_{1}$, id | $L_{1}$. in $=$ L.in; addtype $($ id. entry, L.in $)$ |
| $L \rightarrow$ id | addtype $($ id. entry,L.in $)$ |

addtype () installs $L$. in as the type of the symbol table object pointed to by id. entry (implies a side effect)


## Dependency Graph for float $x, y, z$



## Notes about Inherited Attributes

- Always possible to rewrite a SDD to use only synthesized attributes
- Inherited attributes can be simulated with synthesized attributes and helper functions
- May be more logical to use both synthesized and inherited attributes
- Inherited attributes usually cannot be evaluated by a simple preorder traversal of the parse tree
- Attributes may depend on both left and right siblings!
- Attributes that do not depend on right children can be evaluated by a preorder traversal


## Bottom-up Evaluation of S-Attributed Definitions

- Suppose $A \rightarrow X Y Z$, and semantic rule is $A . a=$ $f(X . x, Y . y, Z . z)$
- Attributes can be computed during bottom-up parsing
- Extend the stack to hold values
- On reduction, value of new synthesized attribute $A$. $a$ is computed from the attributes on the stack



## Example S-Attributed Definition

| Production | Semantic Rules |
| :---: | :--- |
| $L \rightarrow E \$$ | L.val $=E . v a l$ |
| $E \rightarrow E_{1}+T$ | $E . v a l=E_{1} . v a l+T . v a l$ |
| $E$ | E.val $=T . v a l$ |
| $T \rightarrow T_{1} * F$ | T.val $=T_{1} . v a l \times F . v a l$ |
| $T \rightarrow F$ | T.val $=F . v a l$ |
| $F \rightarrow(E)$ | F.val $=E . v a l$ |
| $F \rightarrow$ digit | F.val $=$ digit. lexval |

## Bottom-up Evaluation of S-Attributed Definitions

| Value | Symbols | Action |  |
| :--- | :--- | ---: | :--- |
| $\$$ | $\$$ | $3 * 5+4 \$$ | Shift |
| $\$ 3$ | $\$$ digit | $* 5+4 \$$ | Reduce by $F \rightarrow$ digit |
| $\$ 3$ | $\$ F$ | $* 5+4 \$$ | Reduce by $T \rightarrow F$ |
| $\$ 3$ | $\$ T$ | $* 5+4 \$$ | Shift |
| $\$ 3$ | $\$ T *$ | $5+4 \$$ | Shift |
| $\$ 35$ | $\$ T *$ digit | $+4 \$$ | Reduce by $F \rightarrow$ digit |
| $\$ 35$ | $\$ T * F$ | $+4 \$$ | Reduce by $T \rightarrow T * F$ |
| $\$ 15$ | $\$ T$ | $+4 \$$ | Reduce by $E \rightarrow T$ |
| $\$ 15$ | $\$ E$ | $+4 \$$ | Shift |
| $\$ 15$ | $\$ E+$ | $4 \$$ | Shift |
| $\$ 154$ | $\$ E+$ digit | $\$$ | Reduce by $F \rightarrow$ digit |
| $\$ 154$ | $\$ E+F$ | $\$$ | Reduce by $T \rightarrow F$ |
| $\$ 154$ | $\$ E+T$ | $\$$ | Reduce by $E \rightarrow E+T$ |
| $\$ 19$ | $\$ E$ | $\$$ | $\ldots$ |
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## L-Attributed Definitions

- Each attribute must be either
i. Synthesized, or
ii. Suppose $A \rightarrow X_{1} X_{2} \ldots X_{n}$ and $X_{i} . a$ is an inherited attribute. $X_{i} . a$ can be computed using
a) Only inherited attributes from $A$, or
b) Either inherited or synthesized attributes associated with $X_{1}, \ldots, X_{i-1}$, or
c) Inherited or synthesized attributes
associated with $X_{i}$.

| Production | Semantic Rules |
| :---: | :---: |
| $T \rightarrow F T^{\prime}$ | $\begin{aligned} & T^{\prime} \cdot \mathrm{inh}=F \cdot \mathrm{val} \\ & \text { T.val }=T^{\prime} \cdot \mathrm{syn} \end{aligned}$ |
| $T^{\prime} \rightarrow * F T_{1}^{\prime}$ | $\begin{aligned} & T_{1}^{\prime} \cdot i n h=T^{\prime} \cdot \operatorname{inh} \times F \cdot v a l \\ & T^{\prime} \cdot \operatorname{syn}=T_{1}^{\prime} \cdot s y n \end{aligned}$ |
| $T^{\prime} \rightarrow \epsilon$ | $T^{\prime}$. $s y n=T^{\prime}$. inh |
| $F \rightarrow$ digit | F.val $=$ digit. lexval |

## Are these SDDs S- or L-attributed?

| Production | $\quad$ Semantic Rules |
| :---: | :--- |
| $A \rightarrow B C$ | $A . a=B . b_{1}$ <br> $B . b_{2}=f(A . a, C . c)$ |
|  | $\quad$ Semantic Rules |
| Production | $B . i=f_{1}(A . i)$ <br> $C . i=f_{2}(B . s)$ <br> $A . s=f_{3}(C . s)$ |
| $A \rightarrow B C$ | $\quad$ Semantic Rules |
| Production | $C . i=f_{4}(A . i)$ <br> $B . i=f_{5}(C . s)$ <br> $A . s=f_{6}(B . s)$ |
| $A \rightarrow B C$ |  |

## S-Attributed and L-Attributed Definitions

Every S-attributed grammar is also a L-attributed grammar

All L-attributed grammars are not S-attributed

## Challenges with Attribute Grammars

i. Rules only involve local information (i.e., attributes pertaining to symbols in the production)

- Needs additional attributes and copy rules to use non-local information, which increases memory and run-time overhead
ii. Results can be scattered across attributes in the parse tree
iii. Works in conjunction with a parse tree or an AST
- A compiler implementation may not build either


## Syntax-Directed Translation

## Recap SDDs

- Syntax-directed definition (SDD)
- Defines a set of attributes and translations at every node of the parse tree, output is available at the root
- Functional style which hides implementation details
- Evaluation order is not specified among multiple attributes for a production
- Only requirement is there should not be any circularity


## Associating Semantic Rules with Productions

- Syntax-directed translation (SDT)
- Program fragments are embedded as semantic actions in production body
- Generates code while parsing
- Indicates order in which semantic actions are to be evaluated

$$
\text { rest } \rightarrow+\text { term }\left\{\operatorname{print}(\text { "+") }\} \text { rest }_{1}\right.
$$

- Executable specification of an SDD, easier to implement, and can be more efficient since the compiler can avoid constructing a parse tree and a dependency graph
- Yacc/Bison uses translation schemes


## SDT for Infix to Postfix Translation

| SDD |  | SDT |  |
| :---: | :---: | :---: | :---: |
| Production | Semantic Rule | Production | Semantic Action |
| expr | $\text { expr.code }=$ | expr $\rightarrow$ expr $r_{1}+$ term | $\{\operatorname{print}($ " + ") \} |
| $\rightarrow \operatorname{expr}_{1}+$ term | expr $\mathrm{ra}_{1}$ code \||term.code\|" ${ }^{\text {+ }}$ | expr $\rightarrow$ expr $r_{1}-$ term | $\left\{\operatorname{print}\left({ }^{\prime}-{ }^{\prime \prime}\right)\right.$ \} |
| $\underset{\rightarrow \text { expr }_{1}-\text { term }}{\text { expr }}$ | expr.code = <br> expr.code\||term.code||" - " | expr $\rightarrow$ term |  |
| expr $\rightarrow$ term | expr.code $=$ term.code |  | $\{\operatorname{print}(\text { "0") \} }$ |
| term $\rightarrow 0\|1\| \ldots \mid 9$ | $\begin{aligned} & \text { term. } \operatorname{code}=" 0 " \\ & \text { term. code }=" 1 " \\ & \ldots \\ & \text { term } \cdot \text { code }=" 9 " \end{aligned}$ | term $\rightarrow 0\|1\| \ldots \mid 9$ | $\{\operatorname{print}(" 9 ")\}$ |

## SDT Actions



## SDDs and SDTs



- Evaluation of the semantic rules may
- Generate code
- Save information in the symbol table
- Issue error messages
- Perform any other activity


## Construction of AST for Expressions

- Idea: Construct subtrees for subexpressions by creating an operator and operand nodes
- Internal node: $\operatorname{Node}\left(o p, c_{1}, c_{2}, \ldots, c_{k}\right)$
- Create a node with label op, and $k$ fields for $k$ children
- Leaf node: Leaf(op,val)
- Create a node with label $o p$, and $v a l$ is the lexical value


## Creating an AST

Following sequence of function calls create an AST for $a-4+c$

1. $\quad p_{1}=$ new $\operatorname{Leaf}(\mathrm{id}$, entrya)
2. $p_{2}=$ new $\operatorname{Leaf}($ num, 4)
3. $p_{3}=$ new $\operatorname{Node}\left({ }^{\prime \prime}-{ }^{\prime}, p_{1}, p_{2}\right)$
4. $\quad p_{4}=$ new Leaf(id, entryc)
5. $p_{5}=$ new $\operatorname{Node}\left("+{ }^{\prime \prime}, p_{3}, p_{4}\right)$


## S-Attributed Definition for Constructing Syntax Trees

| Production | Semantic Action |
| :---: | :---: |
| $E \rightarrow E_{1}+T$ | $E . n o d e=$ new Node ( ${ }^{+}$' ${ }^{\prime}$, $E_{1}$. node, $\left.T . n o d e\right)$ |
| $E \rightarrow E_{1}-T$ |  |
| $E \rightarrow T$ | E. node $=$ T.node |
| $T \rightarrow(E)$ | T. node $=$ E.node |
| $T \rightarrow$ id | T. node $=$ new Leaf (id, id. entry) |
| $T \rightarrow$ num | T. node $=$ new Leaf(num, num. val) |

## Construction of AST for $a-4+c$



## Construction of AST for $a-4+c$

$\qquad$


## L-Attributed Definition for Constructing Syntax Trees

| Production | Semantic Action |
| :---: | :---: |
| $E \rightarrow T E^{\prime}$ | $\begin{aligned} & \text { E. node }=E^{\prime} . \text { syn } \\ & E^{\prime} . \text { inh }=T . \text { node } \end{aligned}$ |
| $E^{\prime} \rightarrow+T E_{1}^{\prime}$ | $\begin{aligned} & E_{1}^{\prime} \cdot \text { inh }=\text { new Node }\left("+", E^{\prime} \cdot \text { inh }, T \cdot n o d e\right) \\ & E^{\prime} \cdot \operatorname{syn}=E_{1}^{\prime} \cdot \operatorname{syn} \end{aligned}$ |
| $E^{\prime} \rightarrow-T E_{1}^{\prime}$ | $\begin{aligned} & E_{1}^{\prime} \cdot \text { inh }=\text { new } \operatorname{Node}\left("-", E^{\prime} \cdot \text { inh }, T \cdot n o d e ~\right. \\ & E^{\prime} \cdot \operatorname{syn}=E_{1}^{\prime} \cdot \operatorname{syn} \end{aligned}$ |
| $E^{\prime} \rightarrow \epsilon$ | $E^{\prime}$. syn $=E^{\prime}$. inh |
| $T \rightarrow(E)$ | T. node $=$ E. node |
| $T \rightarrow$ id | T. $n$ ode $=$ new Leaf (id, id. entry) |
| $T \rightarrow$ num | T. $n$ ode $=$ new Leaf(num, num. val) |

## Dependency Graph for $a-4+c$



## Implementing SDTs

- Any SDT can be implemented by

1. building a parse tree
2. performing the actions in a left-to-right depth-first order, i.e., preorder traversal

- SDTs are often implemented during parsing, possibly without a parse tree, provided
- Underlying grammar is LR and the SDD is S-attributed, or
- Underlying grammar is LL and the SDD is L-attributed


## Design of Translation Schemes

- Make all attribute values available when the semantic action is executed
- When semantic action involves only synthesized attributes, the action can be put at the end of the production


## Postfix SDT for the Desk Calculator

- Consider S-attributed SDD for a bottom-up grammar
- We can construct an SDT with actions at the end of each production
- SDT with all actions at the rightend of a production is called postfix SDT

| $L \rightarrow E \$$ | \{print(E.val) \} |
| :---: | :---: |
| $E \rightarrow E_{1}+T$ | $\left\{E . v a l=E_{1} \cdot v a l+T . v a l\right\}$ |
| $E \rightarrow T$ | \{ E.val $=$ T.val $\}$ |
| $T \rightarrow T_{1} * F$ | $\left\{T . v a l=T_{1} . v a l \times F . v a l\right\}$ |
| $T \rightarrow F$ | $\{T . v a l=F . v a l\}$ |
| $F \rightarrow(E)$ | $\{$ F.val $=$ E.val $\}$ |
| $F \rightarrow$ digit | $\{F . v a l=$ digit . exval $\}$ |

## Implementing Postfix SDTs During LR Parsing



## Implementing Postfix SDTs with Bottom-up Parsing

| Production | Semantic Action |
| :---: | :---: |
| $L \rightarrow E \$$ | \{print(stack[top - 1].val); top $=$ top -1$\}$ |
| $E \rightarrow E_{1}+T$ | $\begin{aligned} & \text { \{stack[top }-2] . v a l=\operatorname{stack}[\text { top }-2] . v a l+ \\ & \text { stack[top].val; top }=\text { top }-2 ;\} \end{aligned}$ |
| $E \rightarrow T$ |  |
| $T \rightarrow T_{1} * F$ | $\begin{aligned} & \text { \{stack }[\text { top }-2] \cdot v a l=\text { stack }[\text { top }-2] \cdot v a l \times \\ & \text { stack }[\text { top }] \cdot v a l ; \text { top }=\text { top }-2 ;\} \end{aligned}$ |
| $T \rightarrow F$ |  |
| $F \rightarrow(E)$ | $\begin{aligned} & \{\text { stack }[\text { top }-2] . v a l=\operatorname{stack}[\operatorname{top}-1] . \text { val } ; \text { top }= \\ & \text { top }-2 ;\} \end{aligned}$ |
| $F \rightarrow$ digit | Yacc uses $\$ \$, \$ 1, \$ 2, \ldots$ to refer to the semantic values in the current production |

## SDT with Actions Inside Productions

$$
B \rightarrow X\{a\} Y
$$

- For bottom-up parsing, execute action $a$ as soon as $X$ occurs on top of the stack
- For top-down parsing, execute action $a$ just before expanding nonterminal $Y$ or checking for terminal $Y$ in the input


## Example of an SDT Problematic for Parsing

$L \rightarrow E \$$
$E \rightarrow\{\operatorname{print}("+") ;\} \quad E_{1}+T$
$E \rightarrow T$
$T \rightarrow\{\operatorname{print}(" * ") ;\} \quad T_{1} * F$
$T \rightarrow F$
$F \rightarrow(E)$
$F \rightarrow \operatorname{digit}\{\operatorname{print}($ digit. lexval); $\}$

## Parse Tree with Embedded Actions

- Parse the input and produce a parse tree
- Examine each interior node $N$ for production $A \rightarrow \alpha$
- Add additional children to $N$ for the actions in $\alpha$, in left-to-right order
- Perform a preorder traversal of the tree and execute the action as a node labeled by an action is visited



## Design Rules for L-attributed SDDs

- An inherited attribute for a symbol in the body of a production must be computed in an action before the symbol
- A synthesized attribute for the nonterminal on the LHS can only be computed when all the attributes it references have been computed
- The action is usually put at the end of the production

$$
\begin{aligned}
& S \rightarrow A_{1} A_{2}\left\{A_{1} \cdot i n=1, A_{2} \cdot i n=2\right\} \\
& A \rightarrow a\{\operatorname{print}(A \cdot i n)\}
\end{aligned}
$$



## References

- A. Aho et al. Compilers: Principles, Techniques, and Tools, $2^{\text {nd }}$ edition, 2.3, 5.1-5.4.
- K. Cooper and L. Torczon. Engineering a Compiler, $2^{\text {nd }}$ edition, 4.1, 4.3, 4.4.
- M. Scott. Programming Language Pragmatics, $4^{\text {th }}$ edition, Chapter 4.

