CS 77	1A: Intro to Machin	e Learning,	IIT Kanpur	Quiz I	(24 Jan 2024
Nam Roll N		Dept.			20 marks Page 1 of 2
2. Write 3. Write 4. Don't	ons: uestion paper contains 1 p your name, roll number, o your final answers neatly overwrite/scratch answer t rush to fill in answers. Yo	department abo with a blue/bla s especially in M	ve in block letters neat ck pen . Pencil marks m ICQ – such cases may g	ay get smudged.	SINGLE OF TECHNOLOGY
•	ue-False) Write T or F so give a brief justifica		· •	_	•
1 th	he two hyperplane cla ne same decision bour nswer is T else give a c	ndary if $\mathbf{a} + \mathbf{p}$	= 0 and $b + q = 0$. Give a brief proof	
2 fc	Telbo has learnt a class or some $\mathbf{x}_0 \in \mathbb{R}^2$ then ive brief proof if answ	it must alway	ys be the case that	$\operatorname{sign}(\mathbf{w}^{T}(-\mathbf{x}_0) + \mathbf{k})$	(b) < 0.

Consider $f, g: \mathbb{R} \to \mathbb{R}$ of the form f(x) = ax + b, g(x) = bx + a with a, b > 0. If $a \neq b$, there must exist $x_0, x_1 \in \mathbb{R}$ such that $f(x_0) < g(x_0)$ and $f(x_1) > g(x_1)$. If

your answer is T, give example of x_0 , x_1 in terms of a, b, else give a counter example.

3

Q2. (Sliding parabolas) Consider $f(x) = (x-a)^2 + b$, $g(x) = -(x-p)^2 + q$ and $h(x) = x^3/2$.

Find values of $a, b \in \mathbb{R}$ such that f and h share a tangent at $x = 1$.	a =	b =
Find values of $p, q \in \mathbb{R}$ such that g and h share a tangent at $x = 1$.	p =	q =
Find the value of $f+g$ at $x=1$ i.e., $(f+g)(1)$	(f+g)(1) =	
Find the first derivative of $f+g$ at $x=1$ i.e., $(f+g)'(1)$	(f+g)'(1) =	
Find second derivative of $f+g$ at $x=1$ i.e., $(f+g)^{\prime\prime}(1)$	(f+g)''(1) =	:

Write your answers only in the space provided.

(2+2+1+1+1=7 marks)

Q4. (Vector line-up) Give examples of 4D vectors (fill-in the 4 boxes) with the following properties. Any example will get full marks so long as it satisfies all the properties mentioned in the question. Your answers to the parts a, b, c, d, e may be same/different. (4 x 1 = 4 marks)

- a. A vector $\mathbf{v} \in \mathbb{R}^4$ such that $\mathbf{v} \neq \mathbf{0}$ and \mathbf{v} is perpendicular to both the vectors (1,0,1,1) and (0,1,0,0).
- b. A vector $\mathbf{v} \in \mathbb{R}^4$ with only integer coordinates (at least 2 non-zero coordinates) whose L_2 norm is also an integer.
- c. A vector $\mathbf{v} \in \mathbb{R}^4$ that is perpendicular to its own negative i.e., $\mathbf{v} \perp -\mathbf{v}$.
- d. A point $\mathbf{v} \in \mathbb{R}^4$ with equal L_2 distance from the vectors (1,2,3,4) and (4,3,2,1).

Anything written here will not be graded