Model Selection, Evaluation Metrics, and Learning from Imbalanced Data

Piyush Rai

Introduction to Machine Learning (CS771A)

November 1, 2018



- Today: Model Selection, Evaluation, Learning from Imbalanced Data
- Reinforcement Learning
- Ensemble methods (e.g., boosting)
- Learning with time series data
- Learning with limited supervision, other practical aspects (e.g., debugging ML algorithms)

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Model Selection



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Note: Usually considered in supervised learning contexts but unsupervised learning too faces this issue (e.g., "how many clusters" when doing clustering)

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 - Wastes training data. Typically used when we have plenty of training data

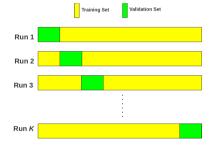
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 - What if there was an unfortunate train/held-out split?

K-fold Cross-Validation

- Create K (e.g., 5 or 10) equal sized partitions of the training data
- Each partition has N/K examples
- ullet Train using $\mathcal{K}-1$ partitions, validate on the remaining partition
- Repeat this K times, each with a different validation partition



K-fold Cross-Validation

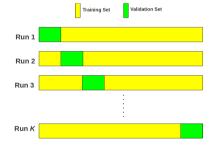
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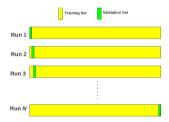
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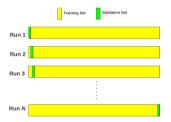


- Average the K validation errors
- Choose the model that gives the smallest average validation error

- Special case of K-fold CV when K = N. Each partition is now a single example
- Train using N-1 examples, validate on the remaining example
- Repeat the same N times, each with a different validation example

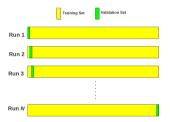


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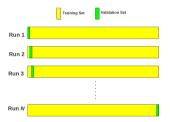
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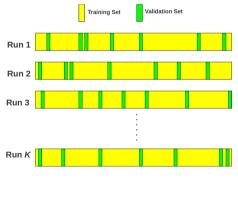


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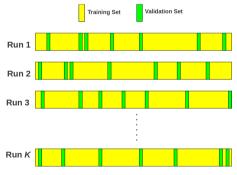


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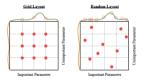
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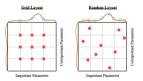
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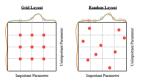
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Finding the best hyperparameters

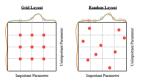
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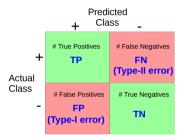
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 - Random Search (see "Random Search for Hyper-Parameter Optimization")
 - Bayesian Optimization (see "Practical Bayesian Optimization of Machine Learning Algorithms")

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Metrics for Evaluating ML Algorithms



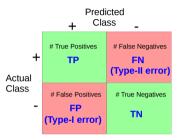
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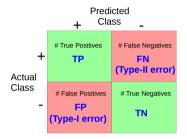
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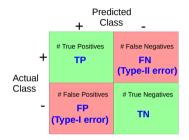


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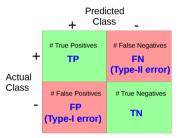
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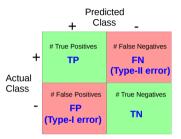
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- Recall = Of all actual positives, what fraction is predicted as positives

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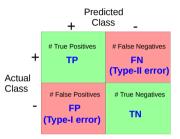


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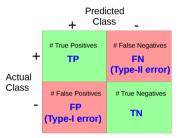


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Precision (P) =
$$\frac{TP}{TP + FP}$$
 Recall (R) = $\frac{TP}{TP + FN}$ F1-score = $\frac{2PR}{P+R}$ (harmonic mean)

- True Positive Rate (TPR) and False Positive Rate (FPR) are also commonly used metrics
- TPR is the same as recall: Fraction of actual positives predicted as positives

$$\mathsf{TPR} = rac{\mathsf{TP}}{\mathsf{TP} + \mathsf{FN}}$$

• FPR is the fraction of actual negatives predicted as positive

$$FPR = \frac{FP}{TN + FP}$$

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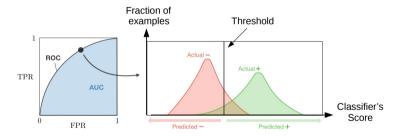
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Intro to Machine Learning (CS771A)

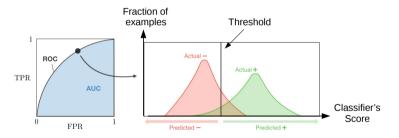
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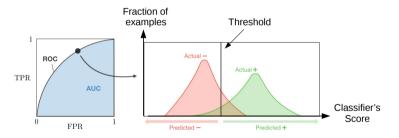


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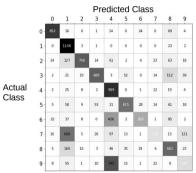
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- Plot of TPR vs FPR for all possible values of the threshold is called Area Under the Receiving Operating Curve (AUCROC or AUC)
- The max AUC score is 1. AUC = 0.5 means close to random.

Multiclass Classification Evaluation Metrics

• For K classes, we will have a $K \times K$ confusion matrix



• Can define precision and recall w.r.t. each class

• Assume true responses $\boldsymbol{y} = [y_1, \dots, y_N]$, predicted responses $\hat{\boldsymbol{y}} = [\hat{y}_1, \dots, \hat{y}_N]$



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- The coefficient of determination metric is defined as

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- \bullet A close to perfect model will have R^2 close to 1
- For linear regression, $SS_{tot} = SS_{reg} + SS_{res} \Rightarrow R^2 = \frac{SS_{reg}}{SS_{tot}}$ (fraction of explained variance)

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 - Accuracy, normalized mutual information (NMI), rand index, purity, etc.



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- External evaluation is often preferred when evaluating unsupervised learning models
 - Use the new representation to train a supervised learning model

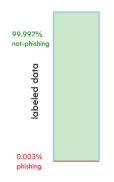
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- Consider binary classification
- Often the classes are highly imbalanced

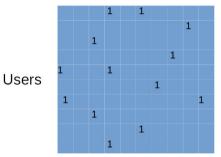


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• Should I feel happy if my classifier gets 99.997% classification accuracy on test data ?

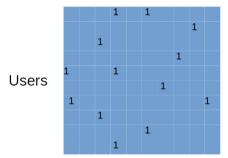
• Other problems can also exhibit imbalance (e.g., binary matrix completion)



Movies

Binary Matrix Completion 0.001 % 1s in the matrix

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Movies

Binary Matrix Completion 0.001 % 1s in the matrix

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 Should I feel happy if my matrix completion model gets 99.999% matrix completion accuracy on the test entries?

- Debatable..
- Scenario 1: 100,000 negative and 1000 positive examples
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- Usually, imbalance is characterized by absolute rather than relative rarity
 - Finding needles in a haystack..



• Any model to minimize the loss, e.g.,

Classification:
$$\hat{\boldsymbol{w}} = \arg \min_{\boldsymbol{w}} \sum_{n=1}^{N} \ell(y_n, \boldsymbol{w}^{\top} \boldsymbol{x}_n)$$

Matrix Completion: $(\hat{\boldsymbol{U}}, \hat{\boldsymbol{V}}) = \arg \min_{\boldsymbol{U}, \boldsymbol{V}} ||\boldsymbol{X} - \boldsymbol{U} \boldsymbol{V}^{\top}||^2$

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 - Thus accuracy alone can't be trusted as the evaluation measure if we care more about predicting minority class (say positive) correctly
 - Need to use metrics such as precision, recall, F1 score, AUC, etc (that specifically care about positives)

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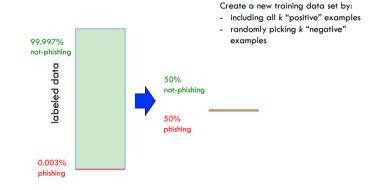
- Modifying the training data (the class distribution)
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- Reweighting can be also seen as a way to modify the loss function

Modifying the Training Data



Undersampling

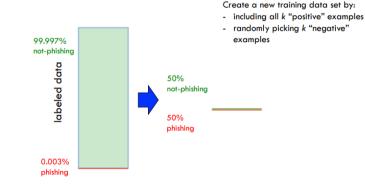


Intro to Machine Learning (CS771A)

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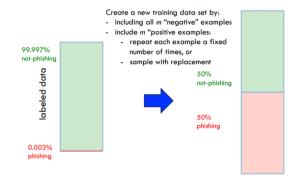
Undersampling



• Throws away a lot of data/information. But efficient to train

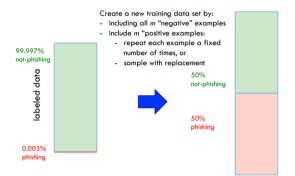
Intro to Machine Learning (CS771A)

Oversampling



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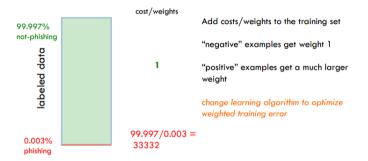
Oversampling



- Th repeated examples simply contribute multiple times to the loss function
- Some oversampling methods (SMOTE) based on creating synthetic examples from minority class

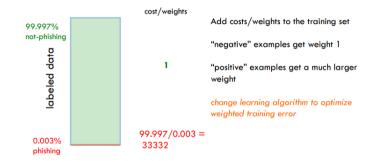
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Reweighting Examples



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• Similar effect as oversampling but is more efficient (because there is no multiplicity of examples)

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- Similar effect as oversampling but is more efficient (because there is no multiplicity of examples)
- Also requires a model that can learn with weighted examples

Intro to Machine Learning (CS771A)

Modifying the Loss Function



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- Why is it a good loss function for imbalanced data?

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Pairwise Loss Functions

• Using pairs with one +ve and one -ve doesn't let one class overwhelm other

$$\sum_{n=1}^{N_+} \sum_{m=1}^{N_-} \ell(f(\boldsymbol{x}_n^+), f(\boldsymbol{x}_m^-)) + \lambda R(f)$$



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 Note: Commonly used pairwise loss functions maximize a proxy of the AUC score (or closely related measures such as F1 score)

• A proxy based on hinge-loss like pairwise loss function for a linear model

$$\ell(\boldsymbol{w}, \boldsymbol{x}_n^+, \boldsymbol{x}_m^-) = \max\{0, 1 - (\boldsymbol{w}^\top \boldsymbol{x}_n^+ - \boldsymbol{w}^\top \boldsymbol{x}_m^-)\} = \max\{0, 1 - \boldsymbol{w}^\top (\boldsymbol{x}_n^+ - \boldsymbol{x}_m^-)\}$$



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- Note: Similar ideas can be used for solving binary matrix factorization and matrix completion problems as well
 - E.g., if matrix entry $X_{nm} = 1$ and $X_{nm'} = -1$ then loss=0 if $\boldsymbol{u}_n^\top \boldsymbol{v}_m > \boldsymbol{u}_n^\top \boldsymbol{v}_{m'}$

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 - Should look at measures such as precision, recall, or other variants that are robust to class imbalance



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- Another way to look at this problem could be as an anomaly detection problem (minority class is anomaly) or density estimation problem

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