

# Death Threshold of L2 Cache Block Classes in CHAR Algorithms

## Tuning Suggestions

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This brief note should be read in conjunction with the proposal on making replacement and bypass algorithms for last-level caches (LLCs) hierarchy-aware [1]. That proposal introduced cache hierarchy-aware replacement (CHAR) and bypass algorithms. One central parameter of these algorithms is the threshold applied to the reuse probability (or hit rate) in a class of cache blocks to decide if the class of blocks is dead. Such blocks can be replaced early in an inclusive LLC or bypassed in an exclusive LLC. A dynamic algorithm for determining this threshold  $t$  is discussed and evaluated in [1]. This algorithm chooses  $t$  such that blocks from classes with hit rates below the prevailing baseline hit rate would be identified as dead. An implementable approximate version of this algorithm is discussed in [1] and reproduced in Equation (1) below.

$$t = \begin{cases} 1/16 & \text{if } E_4 \leq N_E/8 \\ 1/8 & \text{if } N_E/8 < E_4 \leq N_E/4 \\ 1/4 & \text{if } N_E/4 < E_4 \leq N_E/2 \\ 1/2 & \text{if } E_4 > N_E/2 \end{cases} \quad (1)$$

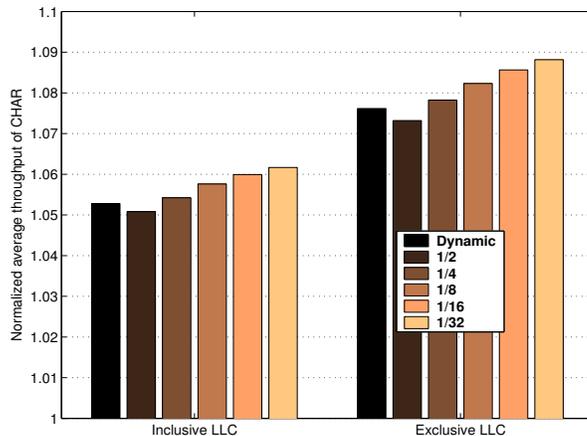
$N_E$  maintains the total number of L2 cache evictions mapping to the LLC sample sets.  $E_4$  maintains the number of L2 cache evictions of blocks belonging to class  $C_4$ . It is possible to replace such a dynamic value of  $t$  by a static predetermined constant  $t$ .

Figure 1 compares the dynamic algorithm with a number of static  $t$  values (1/2, 1/4, 1/8, 1/16, and 1/32) for one hundred four-way multi-programmed workloads with hardware prefetcher enabled (see [1] for configuration details). For both inclusive and exclusive LLCs, the baseline is an inclusive LLC implementing the SRRIP replacement policy [2]. As can be seen, the dynamic policy delivers performance better than static  $t = 1/2$  but worse than  $t = 1/4, 1/8, 1/16, 1/32$  for our choice of workloads. While our dynamic algorithm tries to eliminate blocks from classes with hit rates below the prevailing baseline hit rate, for certain workload classes  $t = 1/2$  can be very aggressive, as can be seen from the static  $t = 1/2$  results.

One possible tuning technique for the dynamic algorithm would be to choose  $t$  such that it eliminates blocks from classes with hit rates below, say,  $1/2^k$ th of the prevailing baseline hit rate. This would lead to the following approximate algorithm.

$$t = \begin{cases} 1/(16 * 2^k) & \text{if } E_4 \leq N_E/8 \\ 1/(8 * 2^k) & \text{if } N_E/8 < E_4 \leq N_E/4 \\ 1/(4 * 2^k) & \text{if } N_E/4 < E_4 \leq N_E/2 \\ 1/(2 * 2^k) & \text{if } E_4 > N_E/2 \end{cases} \quad (2)$$

Therefore,  $k = 1$  would result in  $t$  values ranging from 1/4 to 1/32, while  $k = 2$  would lead to  $t$  values in the range 1/8 to 1/64. The value  $k = 0$  corresponds to the dynamic algorithm discussed in [1].



**Figure 1.** Normalized throughput comparison for static and dynamic  $t$  on one hundred four-way multi-programmed workloads with hardware prefetcher enabled.

Since too small a value of  $t$  may lead to lost opportunities and too large a value may lead to loss in performance due to aggressive death prediction, another alternative approach to tuning the dynamic algorithm would involve fixing a minimum and a maximum allowable  $t$  value, say,  $t_{min}$  and  $t_{max}$ , respectively. Next, we take Equation (2) and choose  $k$  such that  $t_{min}$  equals  $1/(16 * 2^k)$ , i.e., the minimum value of  $t$  in Equation (2). Finally, we merge all the ranges in Equation (2) that have values of  $t$  more than  $t_{max}$  with the range that has value  $t_{max}$ . As an example, suppose  $t_{max}$  is  $1/8$  and  $t_{min}$  is  $1/32$ . This leads to  $k = 1$  and the following dynamic algorithm.

$$t = \begin{cases} 1/32 & \text{if } E_4 \leq N_E/8 \\ 1/16 & \text{if } N_E/8 < E_4 \leq N_E/4 \\ 1/8 & \text{if } E_4 > N_E/4 \end{cases} \quad (3)$$

Similarly, if we set  $t_{max}$  to  $1/8$  and  $t_{min}$  to  $1/16$ , we get the following dynamic algorithm.

$$t = \begin{cases} 1/16 & \text{if } E_4 \leq N_E/8 \\ 1/8 & \text{if } E_4 > N_E/8 \end{cases} \quad (4)$$

In summary, when choosing a value of  $t$  it should be kept in mind that too small a value may lead to performance close to the baseline due to lost opportunities, while too large a value, may lead to loss in performance due to aggressive death prediction. In general, we have found that a small conservative static value of  $t$  works well e.g.,  $t = 1/8, 1/16$ . However, a well-tuned dynamic algorithm may be desirable so that the CHAR policy can adapt to varying workload characteristics. In this brief note, we have proposed a couple of tuning strategies for choosing a dynamic value of  $t$ .

## References

- [1] M. Chaudhuri et al. Introducing Hierarchy-awareness in Replacement and Bypass Algorithms for Last-level Caches. In *Proceedings of the 21st IEEE/ACM International Conference on Parallel Architecture and Compilation Techniques*, pages 293–304, September 2012.
- [2] A. Jaleel et al. High Performance Cache Replacement using Re-reference Interval Prediction (RRIP). In *Proceedings of the 37th International Symposium on Computer Architecture*, pages 60–71, June 2010.