

Program Analysis

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Constant Propagation

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Constant Propagation

- Replace expressions that evaluate to same constant “c” every time they are executed, by the value “c”

DF Framework for ConstProp

- Domain
 - For a single variable v of type t , all possible constant values of type t
 - \top and \perp ?
- Semilattice?

DFF for CP

- NAC: not a constant
 - If variable is inferred not to be a constant
 - Multiple (different valued) defs, non-const defs, assigned an “un-interpreted” value ...
- UNDEF: No definition of the variable is seen yet – nothing known!

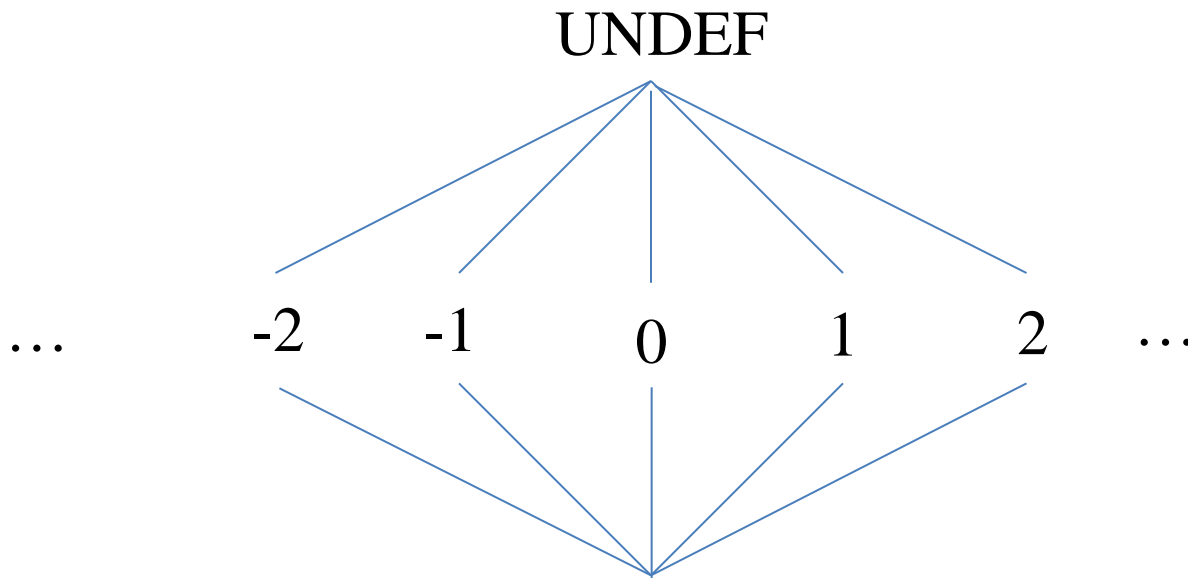
NAC vs UNDEF

- NAC \Rightarrow too many definitions seen to declare the variable is NOT constant
- UNDEF \Rightarrow too few definitions seen to declare anything about the variable
- T is UNDEF; \perp is NAC

CP Meet (\wedge)

- $\text{UNDEF} \wedge c = c$ $\text{NAC} \wedge c = \text{NAC}$
 - Recall $\top \wedge x = x$ and $\perp \wedge x = \perp$
- $c \wedge c = c$
- $c1 \wedge c2 = \text{NAC}$

CP Semilattice



- Infinite Domain, but finite height

CP Semilattice

- Previous figure semilattice for one variable
- CP Semilattice = Product of all such semilattices
- Each semilattice has a **finite** height

OUT Information

(Informal Representation)

1. $x = c // \text{const}$

– $\{x \rightarrow c\}$

2. $x = y + z$

– If $\{y \rightarrow c1, z \rightarrow c2\}$ in IN then $\{x \rightarrow c1+c2\}$

– If $\{y \rightarrow \text{NAC}\}$ in IN then $\{x \rightarrow \text{NAC}\}$

– If $\{z \rightarrow \text{NAC}\}$ in IN then $\{x \rightarrow \text{NAC}\}$

– $\{x \rightarrow \text{UNDEF}\} // y$ is UNDEF or z is UNDEF

3. $x = \langle \text{complicated unhandled expr} \rangle$

– $\{x = \text{NAC}\}$

Monotonicity of CP

- Case analysis on transfer function f
- $NAC \leq c \leq UNDEF$
- Case (1) and (3) has “constant” f
- Case (2):
 - Fix z (One of UNDEF, c_2 , NAC)
 - Vary y over UNDEF, c_1 , NAC
 - Confirm that x does not “increase”
 - Do this for all z 's.
 - Similarly, fix y and vary z .

Nondistributivity of CP

```
B0: ...  
if (...) {  
  B1:   x = 2;  
        y = 3;  
} else {  
  B2:   x = 3;  
        y = 2;  
}  
B3: z = x + y;  
...
```

All paths:

B0-B1-B3

B0-B2-B3

z is 5 along both paths

Meet \wedge results in z = NAC

(Exercise)

MOP: z is a constant 5

MFP: z is NAC

MFP not equal to MOP