

**Answer to B3**

$$\begin{aligned}
 -15 \cos\theta_1 + 15 \cos\theta_2 &= 2.5 \\
 -\cos\theta_1 + \cos\theta_2 &= \frac{1}{6} \dots\dots\dots(1) \\
 15 \sin\theta_1 + 15 \sin\theta_2 &= 12 \\
 -\sin\theta_1 + \sin\theta_2 &= \frac{4}{5} \dots\dots\dots(2)
 \end{aligned}$$

Square and add equations (1) and (2)

$$\begin{aligned}
 2 - 2\cos\theta_1\cos\theta_2 + 2\sin\theta_1\sin\theta_2 &= \frac{16}{25} + \frac{1}{36} \\
 2 - \cos(\theta_1+\theta_2) - \cos(\theta_1-\theta_2) + \cos(\theta_1-\theta_2) - \cos(\theta_1+\theta_2) &= \frac{16}{25} + \frac{1}{36} \\
 2\cos(\theta_1+\theta_2) &= 2 - \frac{16}{25} - \frac{1}{36} \\
 \cos(\theta_1+\theta_2) &= 0.666 \\
 \theta_1+\theta_2 &= 48.2323 \\
 \text{Substitute in (1)} \\
 -\cos(48.2323-\theta_2) + \cos\theta_2 &= \frac{1}{6} \\
 -2\sin(48.2323/2)\sin(\theta_2-48.2323/2) &= \frac{1}{6} \\
 \sin(\theta_2-48.2323/2) &= -0.20395 \\
 \theta_2-48.2323/2 &= -11.7683 \\
 \theta_1 &= 35.88 \\
 \theta_2 &= 12.35
 \end{aligned}$$

$$\begin{aligned}
 20 + 15\cos\theta_3 - 15\cos\theta_4 &= 7.5 \\
 15\cos\theta_3 - 15\cos\theta_4 &= -12.5 \\
 \cos\theta_3 - \cos\theta_4 &= -\frac{5}{6} \dots\dots\dots(3) \\
 15\sin\theta_3 + 15\sin\theta_4 &= 12.5 \\
 \sin\theta_3 + \sin\theta_4 &= \frac{4}{5} \dots\dots\dots(4) \\
 \text{Square and add equations (3) and (4)} \\
 2 - 2\cos\theta_3\cos\theta_4 + 2\sin\theta_3\sin\theta_4 &= \frac{25}{36} + \frac{16}{25} \\
 2 - \cos(\theta_3+\theta_4) - \cos(\theta_3-\theta_4) + \cos(\theta_3-\theta_4) - \cos(\theta_3+\theta_4) &= \frac{25}{36} + \frac{16}{25} \\
 2\cos(\theta_3+\theta_4) &= 2 - \frac{25}{36} - \frac{16}{25} \\
 \cos(\theta_3+\theta_4) &= 0.332 \\
 \theta_3+\theta_4 &= 70.563 \\
 \text{Substitute in (4)} \\
 \sin(70.563-\theta_4) + \sin\theta_4 &= \frac{4}{5} \\
 2\sin(70.563/2)\cos(70.563/2-\theta_4) &= \frac{4}{5} \\
 \cos(70.563/2-\theta_4) &= 0.6925 \\
 35.2815-\theta_4 &= 46.1695 \\
 \theta_4 &= -10.88 \\
 \theta_3 &= 81.44
 \end{aligned}$$

Convention: If we take  $\theta_1, \theta_2, \theta_3$  and  $\theta_4$  anticlockwise position and front arm angles wrt base arm angles then

$$\begin{aligned}
 \theta_1 &= 144.12 \\
 \theta_2 &= 228.23 \\
 \theta_3 &= 81.44 \\
 \text{and } \theta_4 &= 109.44
 \end{aligned}$$