## Introduction to Machine Learning and Probabilistic Modeling

Piyush Rai

Probabilistic Machine Learning (CS772A)

Dec 30, 2015

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- Course website: http://www.cse.iitk.ac.in/users/piyush/courses/ pml\_winter16/PML.html
- Instructor: Piyush Rai (http://www.cse.iitk.ac.in/users/piyush/)
- TAs: Milan Someswar, Vinit Tiwari, Rahul Kumar Patidar
- Discussion site: https://piazza.com/iitk.ac.in/secondsemester2016/cs772a/
- **Background assumed:** basics of linear algebra, multivariate calculus, probability and statistics, optimization, programming (MATLAB, R, Python).

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- 3 homework assignments: 30%, Midterm exam: 20%, Final exam: 20%
- Project: 30% (to be done in groups of 3 students)

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#### • Grading:

- 3 homework assignments: 30%, Midterm exam: 20%, Final exam: 20%
- Project: 30% (to be done in groups of 3 students)
- Note: A really awesome project (e.g., publishable piece of work) may help you automatically get an A grade. You may propose your own project or talk to me for ideas. The project has to be (at least loosely) related to probabilistic ML. More details coming soon.

#### Books

Some books with a bent towards *probabilistic* machine learning:



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Some other books on machine learning:



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#### **Books**

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Some other books on machine learning:



Not shown: many excellent books on special topics (kernel methods, online learning, Bayesian learning, deep learning, etc.). Ask me if you want to know.

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## Intro to Machine Learning

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• Creating programs that can automatically learn rules from data *"Field of study that gives computers the ability to learn without being explicitly programmed"*(Arthur Samuel, 1959)

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• Machine Learning (ML): Learn rules by looking at the data



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• Machine Learning (ML): Learn rules by looking at the data



• Learned rules must generalize (do well) on future "test" data (idea of generalization; more on this later)

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#### Machine Learning in the real-world

Broadly applicable in many domains (e.g., finance, robotics, bioinformatics, computer vision, NLP, databases, systems, etc.). Some applications:

- Information retrieval (text, visual, and multimedia searches)
- Machine Translation
- Question Answering
- Social networks
- Recommender systems (Amazon, Netflix, etc.)
- Speech/handwriting/object recognition
- Ad placement on websites
- Credit-card fraud detection
- Weather prediction
- Autonomous vehicles (self-driving cars)
- Healthcare and life-sciences
- .. and many more applications in sciences and engineering

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## Data and Data Representation..

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- ML algorithms work with data represented as a set of features/attributes
- One popular representation: bag-of-features



Picture courtesy: Svetlana Lazebnik

- ML algorithms work with data represented as a set of features/attributes
- One popular representation: bag-of-features



• The idea: Decide features to represent data (becomes our feature vocabulary)

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Picture courtesy: Svetlana Lazebnik

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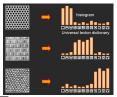
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• The idea: Decide features to represent data (becomes our feature vocabulary)

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• Now represent each example using the frequency of each feature



Picture courtesy: Svetlana Lazebnik

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Another example: representing text data. Consider the following sentences:

- John likes to watch movies
- Mary likes movies too
- John also likes football

The feature vocabulary consists of 8 unique words

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Here is the **bag-of-words** feature representation of these 3 sentences

	/John	likes	to	watch	movies	Mary	too	also	football
Sentence 1								0	- 1
Sentence 2	0	1	0	0	1	1	1	0	0
Sentence 3	1	1	0	0	0	0	0	1	1 )

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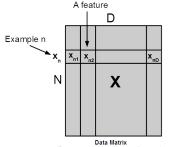
Note: Not necessarily the most optimal/most expressive feature representation

Feature representation learning is a very active area of research in ML (there is even a dedicated conference on this topic: ICLR)

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We will (usually) assume that:

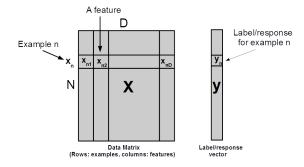
- X denotes data in form of an  $N \times D$  feature matrix
- N examples, D features to represent each example
- Each row is an example, each column is a feature
- $x_n$  denotes the *n*-th example (a vector of length *D*)



Data Matrix (Rows: examples, columns: features)

We will (usually) assume that:

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- y denotes labels/responses in form of an  $N \times 1$  label/response vector
- $y_n$  denotes label/response of the *n*-th example  $x_n$

Probabilistic Machine Learning (CS772A)

# Types of Machine Learning problems..

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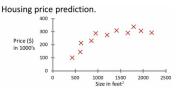
- Given: Training data as labeled examples  $\{(x_1, y_1), \dots, (x_N, y_N)\}$
- Goal: Learn a rule ("function"  $f : x \to y$ ) to predict outputs y from inputs x

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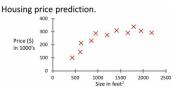
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  - **Continuous-/real-valued** (Regression problem). Example: when *y* is the price of a stock, price of a house, USD/rupee conversion rate, etc.



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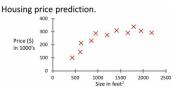


• **Discrete-valued** (Classification problem): Example: when y is the binary 0/1 label (spam/normal) of an email, label (0-9) of a handwritten digit, etc.

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				17711
				22322
				33333
				44449
				55555
				66666
				11177
				88884
1999	1991	1999	9999	99999

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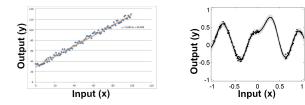
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• Many other variants (structured-prediction, multi-label learning, ordinal regression, ranking, etc.), depending on the type of label y

#### Supervised Learning: Pictorially

• Regression (linear/nonlinear): fitting a line/curve

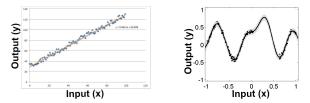


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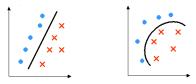
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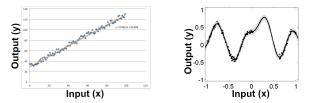


• Classification (linear/nonlinear): finding a separator

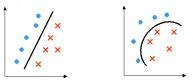


#### Supervised Learning: Pictorially

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• Generalization is crucial (must do well on test data)

#### Generalization

• Simple hypotheses/rules are preferred over more complex ones



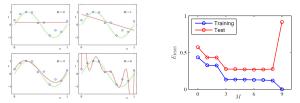
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#### Generalization

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• Simple hypotheses/rules tend to generalize better



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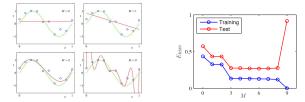
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#### Generalization

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• Desired: hypotheses that are not too simple, not too complex

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- Goal: Learn the instrinsic *structure* in the data.

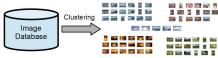
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  - Data clustering (grouping similar things together)



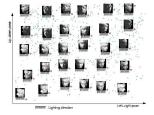
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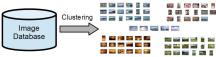
• Dimensionality reduction, embedding, or manifold learning

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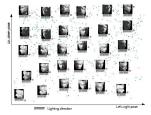


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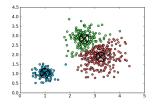
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 Also very useful for summarizing/compressing data. Often also used as a preprocessing step for many supervised learning algorithms (e.g., to extract good features, to speed up the algorithms, etc.)

### **Unsupervised Learning: Pictorially**

• Clustering: Find some "centers" and assign each data point to its "closest" center



• Dimensionality reduction: Find a lower-dimensional subspace that the data approximately lives on



# Other popular Machine Learning paradigms

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• Learning with labeled+unlabeled data

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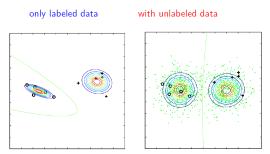
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  - Labeled data is expensive. Unlabeled data comes (almost) for free!

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- Learning with labeled+unlabeled data
- Why is Semi-supervised Learning useful?
  - Labeled data is expensive. Unlabeled data comes (almost) for free!
  - Unlabeled data can provide valuable information about the distribution of data (e.g., where might the low-density regions or the class separator lie)



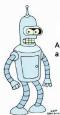
from [Semi-Supervised Learning, ICML 2007 Tutorial; Xiaojin Zhu]

#### **Active Learning**

• The learner can interactively ask for labels of most informative examples



raw unlabeled data  $x_1, x_2, x_3, \ldots$ 



Assumes some small amount of initial labeled training data

active learner induces a classifier

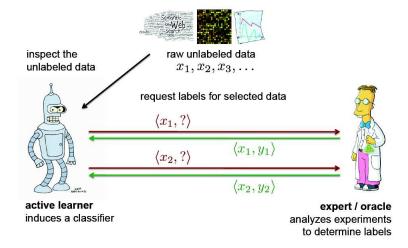


expert / oracle analyzes experiments to determine labels

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## **Active Learning**

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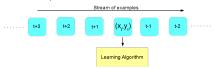


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## Some Other Learning Paradigms

#### • Online Learning

• Learning with one example (or a small minibatch of examples) at a time

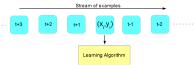


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#### • Online Learning

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#### • Reinforcement Learning

• Learning a "policy" by performing actions and getting rewards



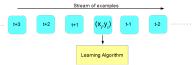
Reinforcement Learning Setup

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Reinforcement Learning Setup

#### • Transfer/Multitask Learning

• Leveraging knowledge of solving one problem to solve a new problem



# On to Probabilistic Machine Learning..

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• Assume data  $\mathbf{X} = \{\mathbf{x}_n\}_{n=1}^N$  generated from a probability distribution  $p(\mathbf{x}|\theta)$ , in an i.i.d. (independent and identically distributed) fashion

$$x_1, \ldots, x_N \sim p(x|\theta)$$

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- Assumptions about parameter  $\theta$  can be encoded via a prior distribution  $p(\theta)$ 
  - Also corresponds to imposing a regularizer over  $\theta$  (helps in generalization)

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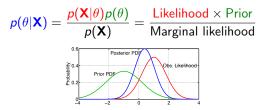
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- Goal: To estimate parameter  $\theta$ , given data X
- Variations of this general view subsume most machine learning problems
  - Regression, classification, clustering, dimensionality reduction, etc.

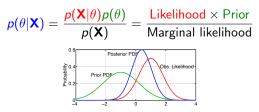
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• Can use Bayes rule to estimate the posterior distribution over parameters



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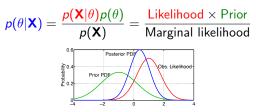
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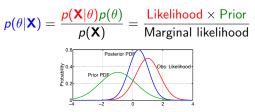
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• Maximum likelihood estimation (MLE)

$$\hat{\theta} = \arg \max_{\theta} p(\mathbf{X}|\theta)$$

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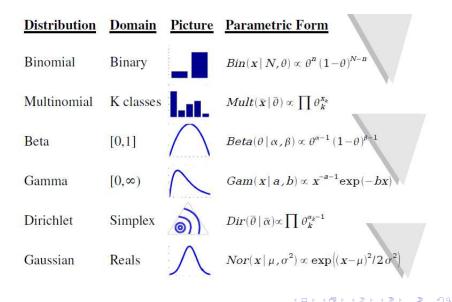
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Maximum-a-Posteriori (MAP) estimation

$$\hat{\theta} = \arg \max_{\theta} p(\theta | \mathbf{X}) = \arg \max_{\theta} p(\mathbf{X} | \theta) p(\theta)$$

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#### Some common probability distributions



# Some Examples of Probabilistic Modeling in Machine Learning

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- Consider regression/classification. Training data  $\{(x_1, y_1), \dots, (x_N, y_N)\}$
- Goal: Learn a function to predict outputs y from inputs x
- Model the output/response/label as a probability distribution

$$\boldsymbol{y}_1,\ldots,\boldsymbol{y}_N\sim p(\boldsymbol{y}|\boldsymbol{x},\theta)$$



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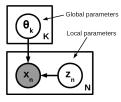
• Can now make probabilistic predictions for new data  $x_*$  using heta

$$p(\boldsymbol{y}_*|\boldsymbol{x}_*, \theta)$$
 or  $p(\boldsymbol{y}_*|\boldsymbol{x}_*)$ 

Probabilistic Machine Learning (CS772A)

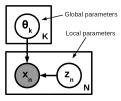
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- Consider clustering or dimensionality reduction problems
- Each data point  $x_n$  assumed to be generated via some latent variable  $z_n$  and parameters  $\theta$



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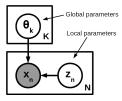
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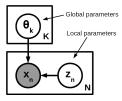
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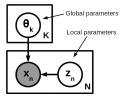
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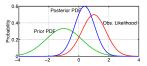
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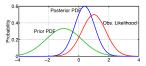
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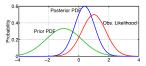
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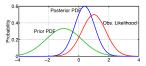
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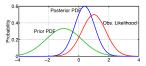
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- Can handle missing and noisy data in a principled way
- Easy/more natural to do semi-supervised learning, active learning, etc.
- Can generate (synthesize) data by simulating from the data distribution

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• Hyperparameters can be learned from data (need not be tuned)

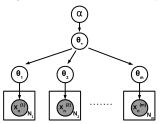


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• Simple models can be neatly combined to solve complex problems

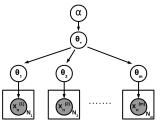


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• Many other benefits. Highly recommended to read this article from Nature: http://www.cse.iitk.ac.in/users/piyush/courses/pml\_winter16/ nature14541.pdf

# **Course Outline**

- Basics of probabilistic modeling and inference
- Probabilistic models for:
  - Regression and classification
  - Clustering
  - Dimensionality reduction
  - Matrix factorization and matrix completion
  - Time-series data modeling
- Bayesian learning and approximate inference
- Deep Learning
- .. and possibly some other topics of common interest

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Next class: Maths refresher. Common probability distributions and their properties

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